## End-to-End Bayesian Entity Resolution

#### Rebecca C. Steorts

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Duke University and U.S. Census Bureau

This work is supported by NSF CAREER Award 1652431.

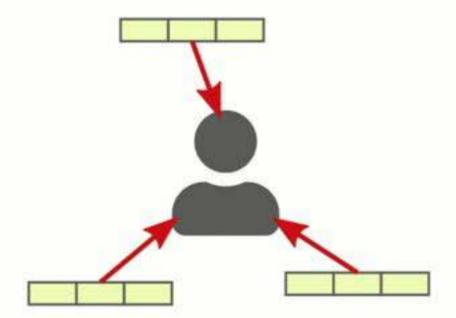
September 6, 2019

# Entity resolution

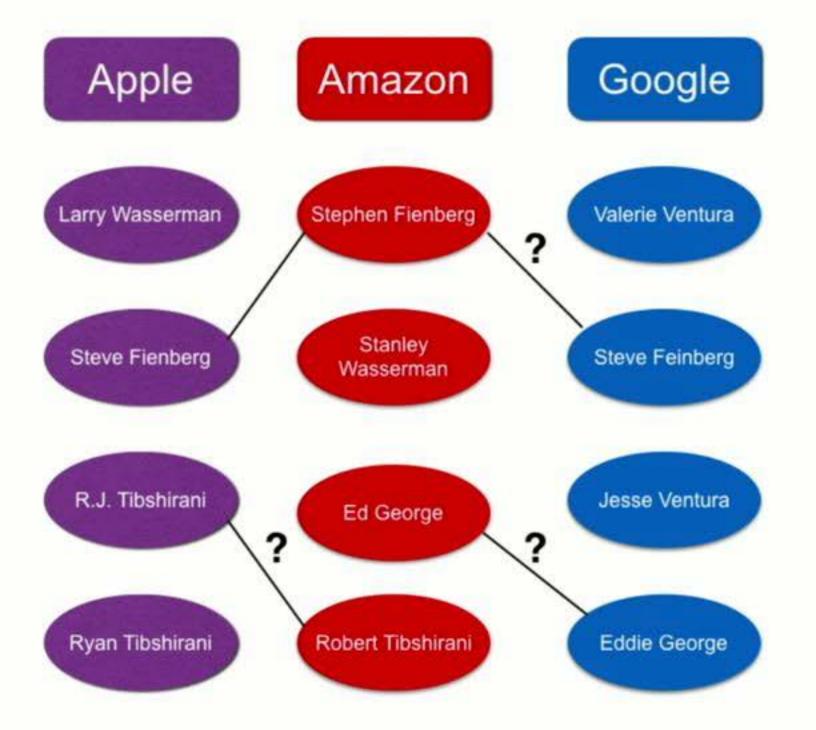
Identifying records across and/or within data sources that refer to the same entities

#### Also known as:

- record linkage
- data matching
- de-duplication
- data integration



# The entity resolution graph



# The node of Larry Wasserman

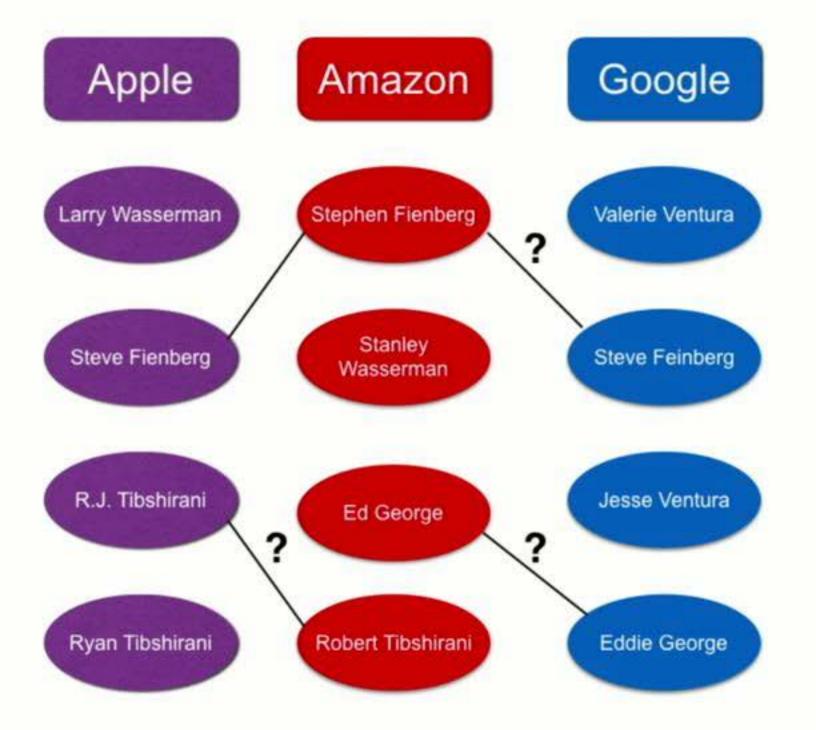


# The node of Larry Wasserman



1014 Murray Hill Avenue Pittsburgh, PA 15217 412-361-3146

# The entity resolution graph



Steve Feinberg

240 Collins Dr Pittsburgh PA 15235 50-54 412-793-3313



537 N Neville St Apt 5d Pittsburgh PA 15213 65+ 412-683-5599



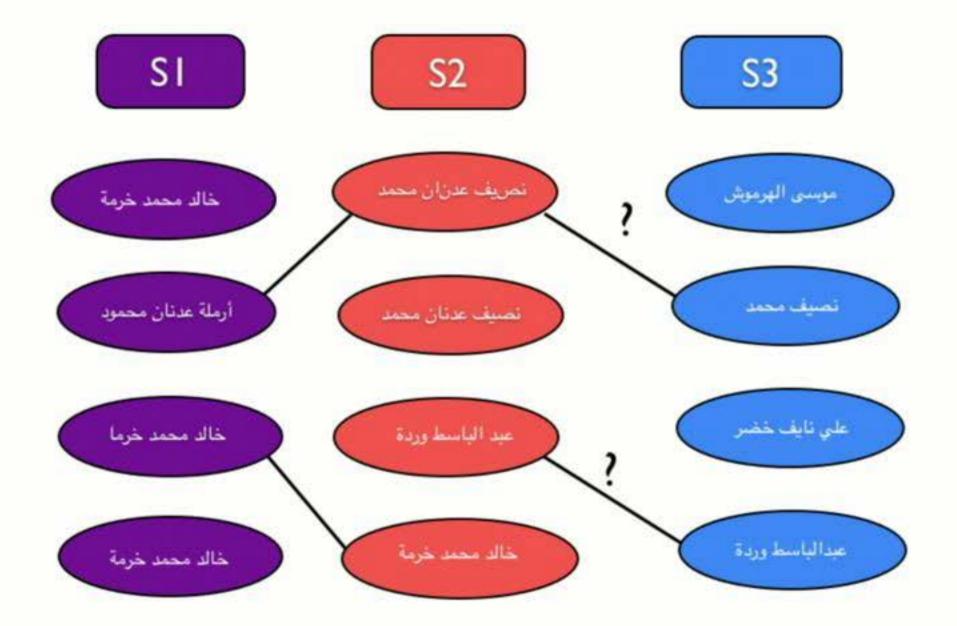
240 Collins Dr Pittsburgh PA 15235 50-54 412-793-3313



537 N Neville St Apt 5d Pittsburgh PA 15213 65+ 412-683-5599

These are clearly not the same Steve Fienberg!

# Syrian Civil War



# **Entity Resolution**

Why is entity resolution difficult?

# Goals of Entity Resolution

Suppose that we have a total of N records in k databases.

- 1 We seek models that are much less than  $O(N^k)$ .
- We seek models that are reliable, accurate, fit the data well, and account for the uncertainty of the model.
- We seek models and algorithms to handle unbalanced data (containing duplications).

### Established ER methods

Common unsupervised methods in statistics:

- probabilistic linking (Fellegi-Sunter theory)
- 2 deterministic linking

#### Established ER methods

#### Common unsupervised methods in statistics:

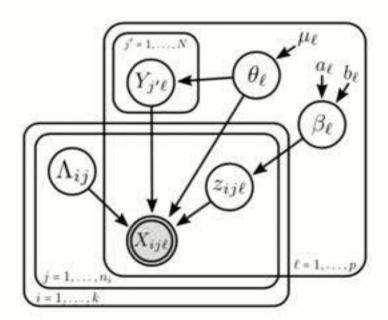
- probabilistic linking (Fellegi-Sunter theory)
- 2 deterministic linking

#### Drawbacks:

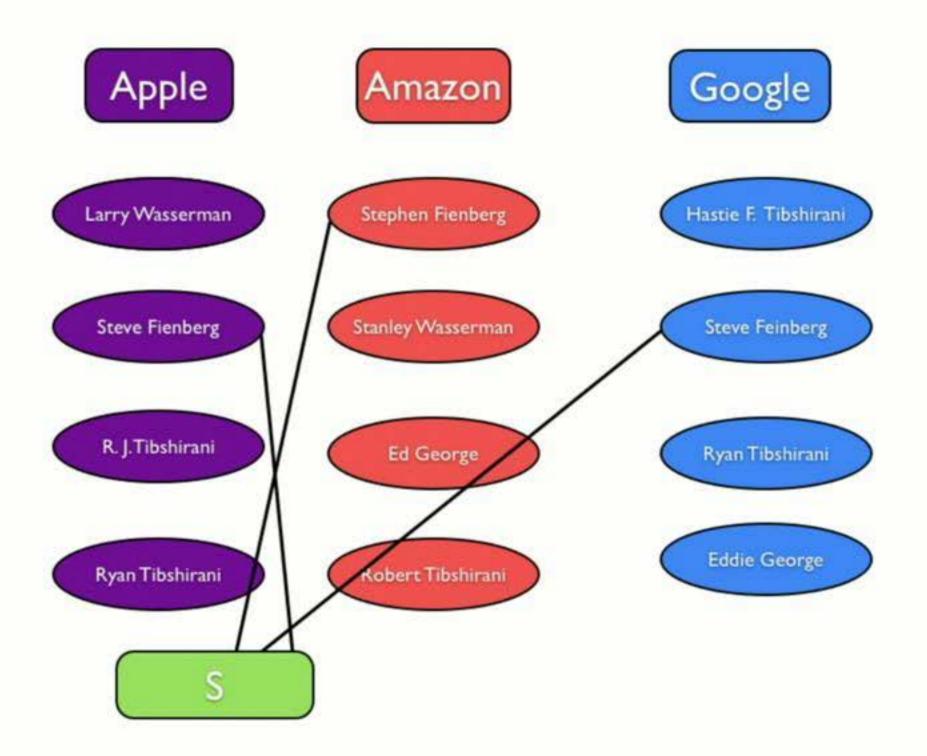
- pairs of records are assessed independently
- awkward post-processing step (transitive closure)
- subjectivity in setting the decision threshold
- lack of uncertainty quantification
- scalability achieved through deterministic blocking

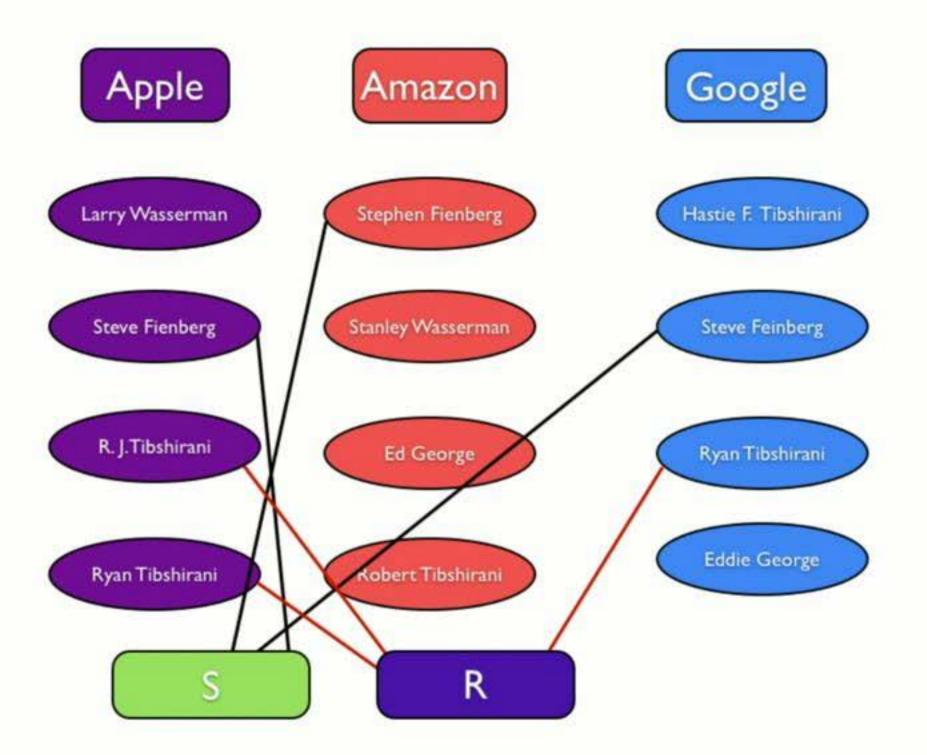
- Dealing with big data means merging large, noisy databases.
  - Such databases have severe amounts of noise.
- Entity resolution requires sophisticated graph structures.
   [Gutman et. al (2013)].
  - One approach is to use a bipartite graph for latent entities.
  - Never link records to records.

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- Computational speed-ups: eliminate low-probability matches.

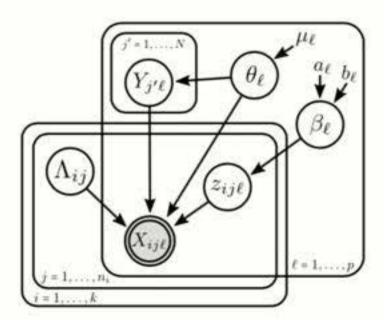


[Tancredi and Liseo (2011), **RCS**, Hall, Fienberg (2014, 2016); Sadinle (2014, 2016), **RCS** (2015), **RCS** et al. (2017), (2018)].

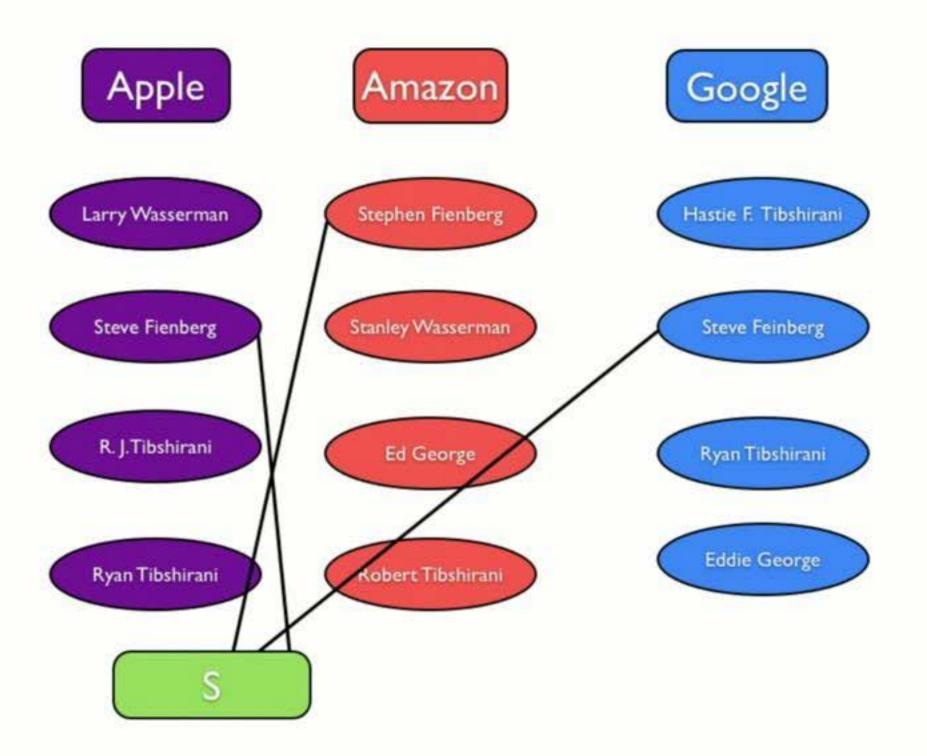




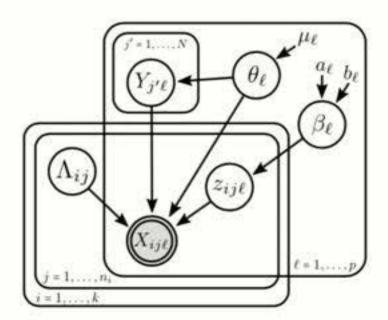
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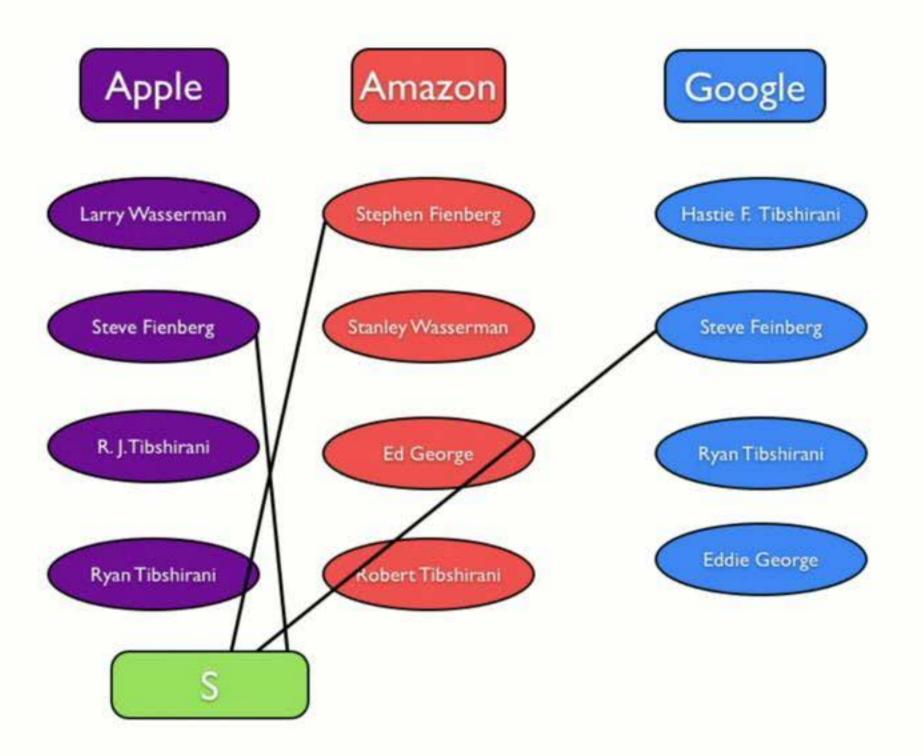
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### Our Goal

Scaling Bayesian ER methods to millions of records without sacrificing accuracy and crucially giving uncertainty of the ER task

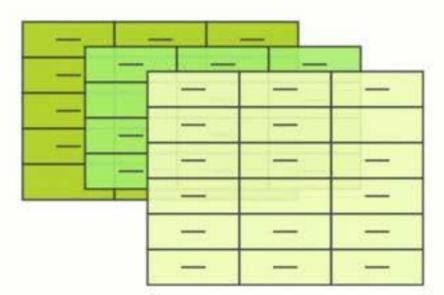
- Incorporating auxiliary partitions that induce conditional independencies between the entities. This enables distributed inference at the partition-level, while crucially preserving the marginal posterior of the original model.
- 2 A partition function (responsible for partitioning the entities), which groups similar entities together while achieving well-balanced partitions.
- 3 Application of partially-collapsed Gibbs sampling in the context of distributed computing.
- 4 Improving computational efficiency:
  - a) Sub-quadratic algorithm for updating links based on indexing.
  - b) Truncation of the attribute similarities.
  - c) Perturbation sampling algorithm for updating the entity attributes, which relies on the Vose-Alias method.

Marchant, RCS, Kaplan, Rubinstein, and Elazar (2019).

# Problem setup

#### Key assumptions:

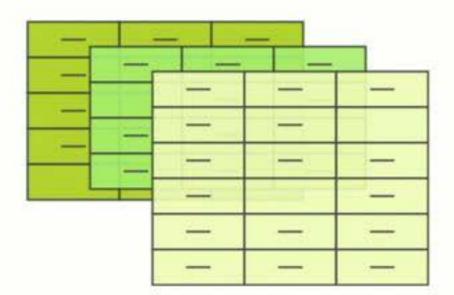
- multiple tables/sources
- duplicates within and across tables
- attributes are aligned
- attributes are discrete
- some missing values
- no ground truth (unsupervised)



### Problem setup

#### Key assumptions:

- multiple tables/sources
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- attributes are discrete
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- no ground truth (unsupervised)

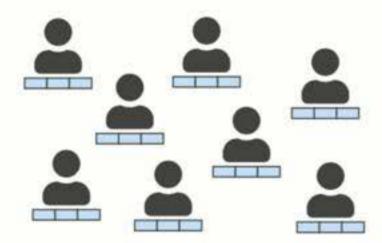


Output: approximate posterior distribution over the linkage structure

#### Latent Entities

- Fixed population of entities  $\mathcal{E} = \{1, \dots, E\}$
- Entity attribute a has a finite domain with distribution  $\phi_a$
- Generate the value for attribute
   a of entity e by

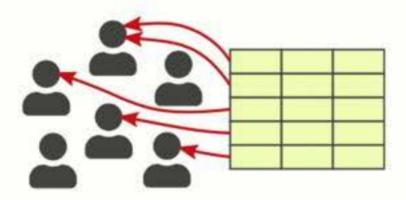
 $y_{ea} \sim \mathsf{Discrete}(\phi_a)$ 



#### Linkage structure

• Record r in table t is linked to an entity  $\lambda_{tr} \in \mathcal{E}$  uniformly at random, viz.

 $\lambda_{tr} \sim \mathsf{DiscreteUniform}(\mathcal{E})$ 



 A distortion probability is associated with each attribute a and table t

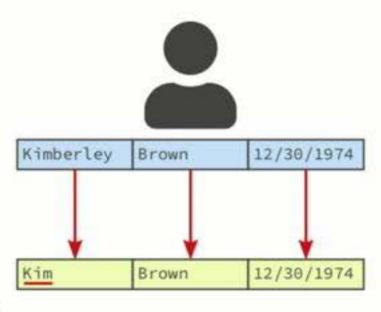
$$\theta_{ta} \sim \mathsf{Beta}(\alpha_{\mathsf{a}}, \beta_{\mathsf{a}})$$

 The value for attribute a of record r in table t follows a hit-miss model

$$egin{aligned} z_{tra} | heta_{ta} &\sim \mathsf{Bernoulli}( heta_{ta}) \ x_{tra} | z_{tra}, y_{\lambda_{tr}a} &\sim (1-z_{tra}) \delta(y_{\lambda_{tr}a}) \ &+ z_{tra} \, \mathsf{Discrete}(\psi_a[y_{\lambda_{tr}a}]) \end{aligned}$$

 Distortion distribution depends on similarity function sim<sub>a</sub>(·,·):

$$\psi_a[y](x) \propto \phi_a(x) \exp(\sin_a(y,x))$$



# d-blink: a more general and scalable model

We propose a distributed version of blink called d-blink

→ distributed, more general model, faster inference algorithms

 A distortion probability is associated with each attribute a and table t

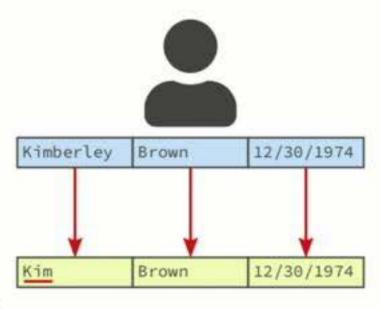
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### d-blink: a more general and scalable model

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#### Modeling differences in d-blink

- Supports missing record values (MCAR)
- Supports arbitrary attribute similarity functions (one for each attribute)
- Incorporates a kind of "blocking": auxiliary partitions of the latent entities (not records)

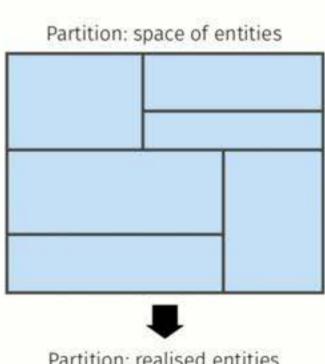
## Auxiliary partitions

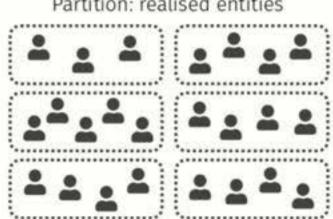
- Enables distributed inference
- Crucially leaves the marginal posterior unchanged
- Partition the space of entities  $\mathcal{V}_{\otimes} = \bigotimes_a \mathcal{V}_a$  using a deterministic function

$$\texttt{PartFn}: \mathcal{V}_{\otimes} \rightarrow \{1, \dots, P\}$$

• Update the model: now record r in table t is assigned to a partition  $\gamma_{tr}$ , then to an entity  $\lambda_{tr}$  within the partition

$$\gamma_{tr}|\mathbf{Y} \sim \mathsf{Discrete}\bigg(\frac{|\mathcal{E}_1|}{|\mathcal{E}|}, \dots, \frac{|\mathcal{E}_P|}{|\mathcal{E}|}\bigg)$$
 $\lambda_{tr}|\gamma_{tr} \sim \mathsf{DiscreteUniform}(\mathcal{E}_{\gamma_{tr}})$ 





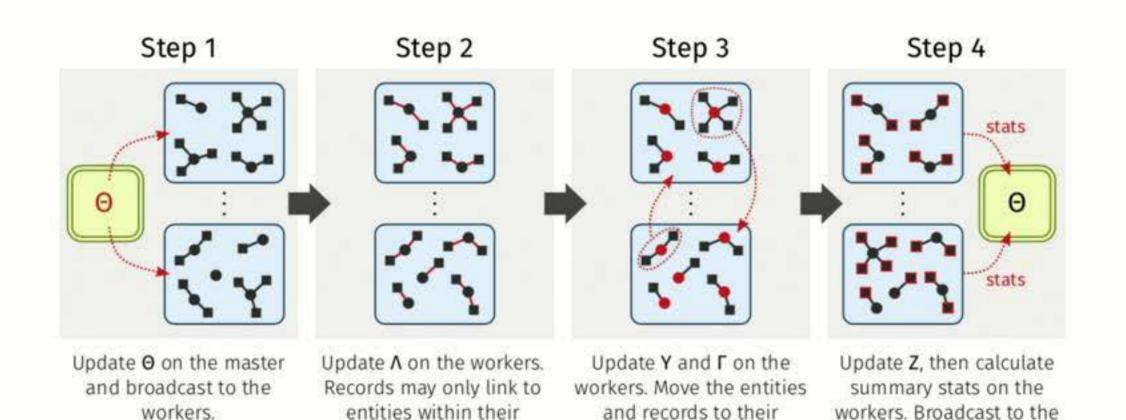
#### Distributed Markov chain Monte Carlo

Since the posterior for the linkage structure  $p(\Lambda|X)$  is not tractable, we resort to approximate inference.

We propose an MCMC algorithm based on the partially-collapsed Gibbs framework (van Dyk and Park, 2008):

- regular Gibbs updates for the distortion probabilities  $\theta_{ta}$ , distortion indicators  $z_{tra}$  and links  $\lambda_{tr}$
- "marginalization" and "trimming" are applied to jointly update the entity attributes  $y_{ea}$  and the partition assignments for the linked records
- order of the updates is important (to preserve the stationary distribution)

### Distributed Markov chain Monte Carlo



newly-assigned partitions.

assigned partitions.

master.

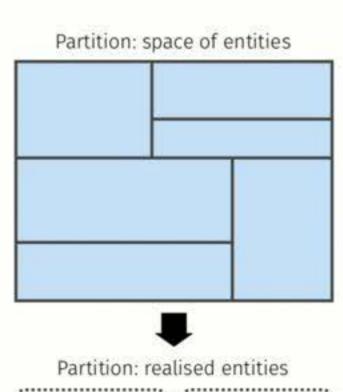
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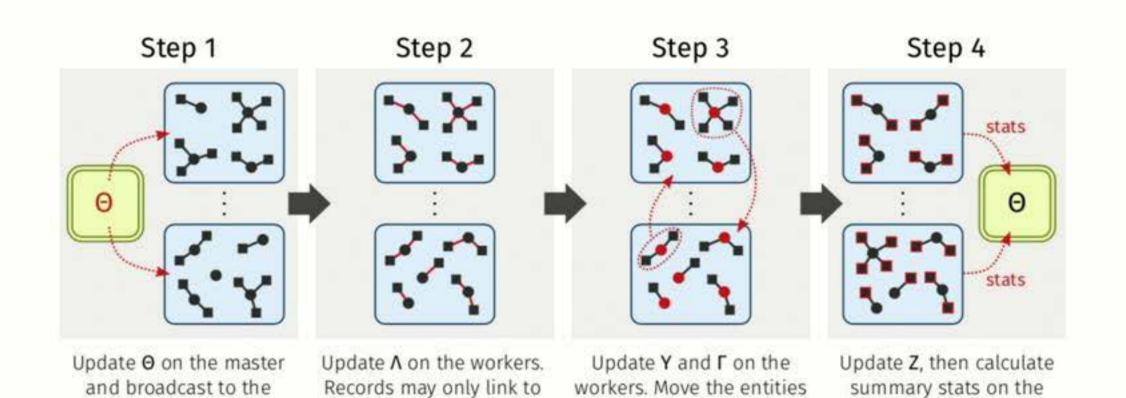
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### Distributed Markov chain Monte Carlo



and records to their

newly-assigned partitions.

entities within their

assigned partitions.

workers.

workers. Broadcast to the

master.

## Tricks for speeding up inference

Two main bottlenecks:

- 1 linkage structure update  $\mathcal{O}(\# \text{ records} \times \# \text{ entities})$
- 2 entity attribute update  $\mathcal{O}(\#$  entities  $\times$  domain size)

## Tricks for speeding up inference

#### Two main bottlenecks:

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#### Solutions:

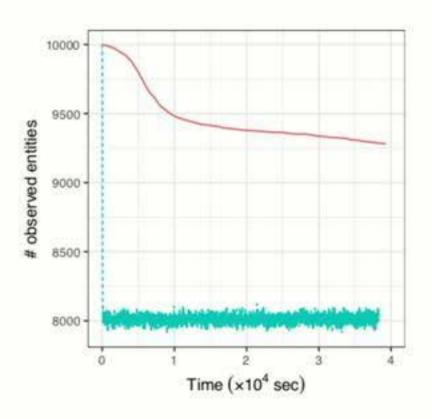
- ① Indexing: Maintain indices from "entity attributes → entities" and "entities → linked records." This allows us to prune candidate links for a record
- 2 Thresholding similarity scores
- 3 Express the distribution for the entity attribute update as a two-component perturbation mixture model

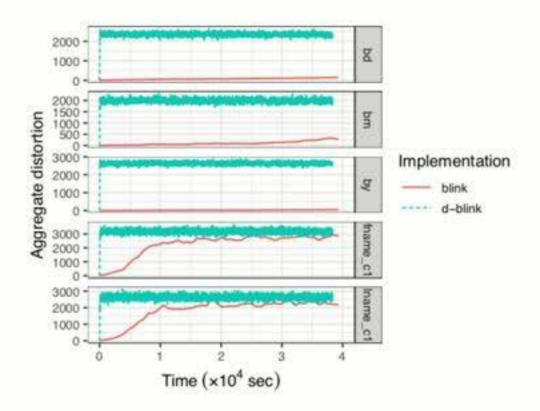
## Experiments

- ABSEmployee. A synthetic data set used internally for linkage experiments by the ABS.
- NCVR. Two snapshots from the North Carolina Voter Registration database taken two months apart.
- NLTCS. A subset of the National Long-Term Care Survey comprising the 1982, 1989 and 1994 waves.
- SHIW0810. A subset from the Bank of Italy's Survey on Household Income and Wealth comprising the 2008 and 2010 waves.
- RLdata10000. A synthetic data set provided with the RecordLinkage R package.

## Convergence of d-blink versus blink

We examined the rate of convergence of d-blink versus blink on RLdata10000 without partitioning.





d-blink converges rapidly, however blink fails to reach the equilibrium distribution within 11 hours.

## Experiments

- Implemented d-blink and baselines in Apache Spark
- Ran experiments on a local server and Amazon EMR
- (Mostly) used a sample size of 10<sup>3</sup> after burnin (of 10<sup>3</sup> iterations) and thinning (keeping every 10th iteration)
- 3 real and 2 synthetic data sets

Data set	# records	# tables	# entities	# attributes		
				categorical	string	
* ABSEmployee	600,000	3	400,000	4	0	
NCVR	448,134	2	296,433	3	3	
NLTCS	57,077	3	34,945	6	0	
SHIW0810	39,743	2	28,584	8	0	
* RLdata10000	10,000	1	9,000	2	3	

Table: Assessment of the pairwise linkage performance for dblink and FS method as our baseline. We note that FS is supervised and does not propagate the entity resolution error exactly compared to dblink.<sup>1</sup>

Data set	Method	Pairwise measure					
		Precision	Recall	F1-score			
ADOR 3	dblink	0.9943	0.8867	0.9374			
ABSEmployee	Fellegi-Sunter (100)	0.9964	0.9510	0.9736			
	Fellegi-Sunter (10)	0.4321	0.6034	0.9736			
	dblink	0.9179	0.9654	0.9411			
NCVR	Fellegi-Sunter (100)	0.8989	0.9974	0.9456			
	Fellegi-Sunter (10)	0.8989	0.9974	0.9456			
NI TOO	dblink	0.8363	0.9102	0.8717			
NLTCS	Fellegi-Sunter (100)	0.7969	0.9959	0.8853			
	Fellegi-Sunter (10)	0.1902	0.9999	0.3196			

<sup>&</sup>lt;sup>1</sup>Comparisons to other semi-supervised methods are the same.

### Posterior Bias Plot

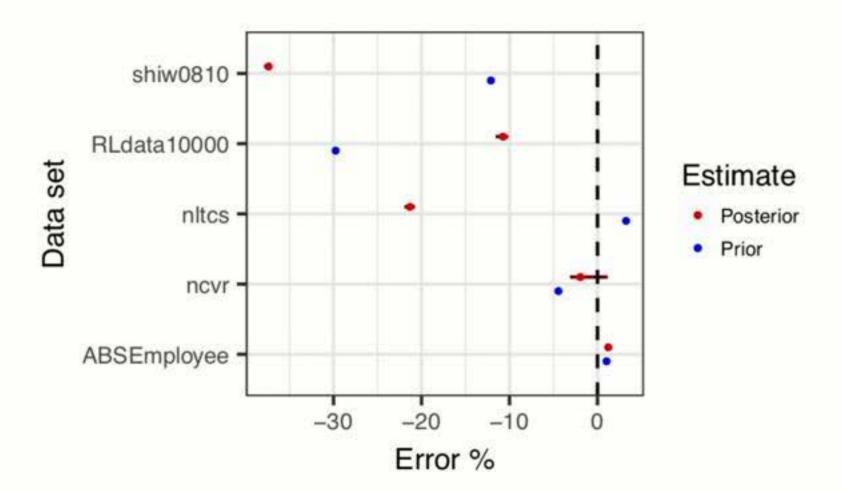
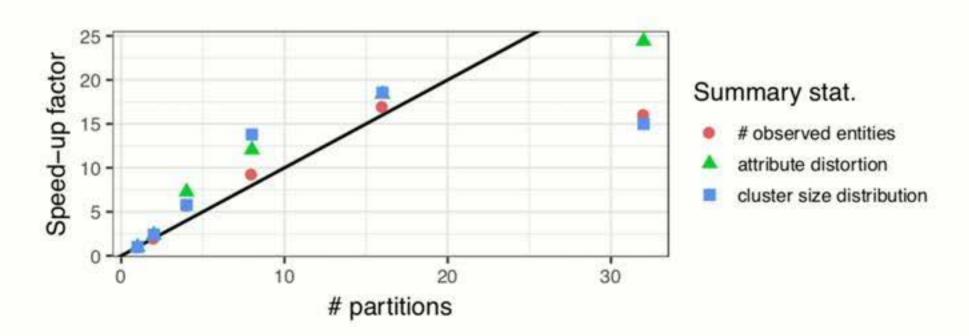


Figure: Error in the posterior and prior estimates for the number of observed entities for d-blink. The results show that the posterior estimate is very sharp and typically underestimates the true number, which is consistent with **RCS**, Hall, Fienberg (2016).

## Does partitioning result in efficiency gains?

- Measure efficiency using ESS rate—the effective sample size generated per unit time
- Speed-up factor is the ESS rate relative to a baseline without partitioning
- Observe a near-linear speed-up for the NLTCS data set (tapering off beyond  $\sim$  20 partitions)



How does our approach handle data with little or no training data from a real application?

### El Salvadoran Conflict

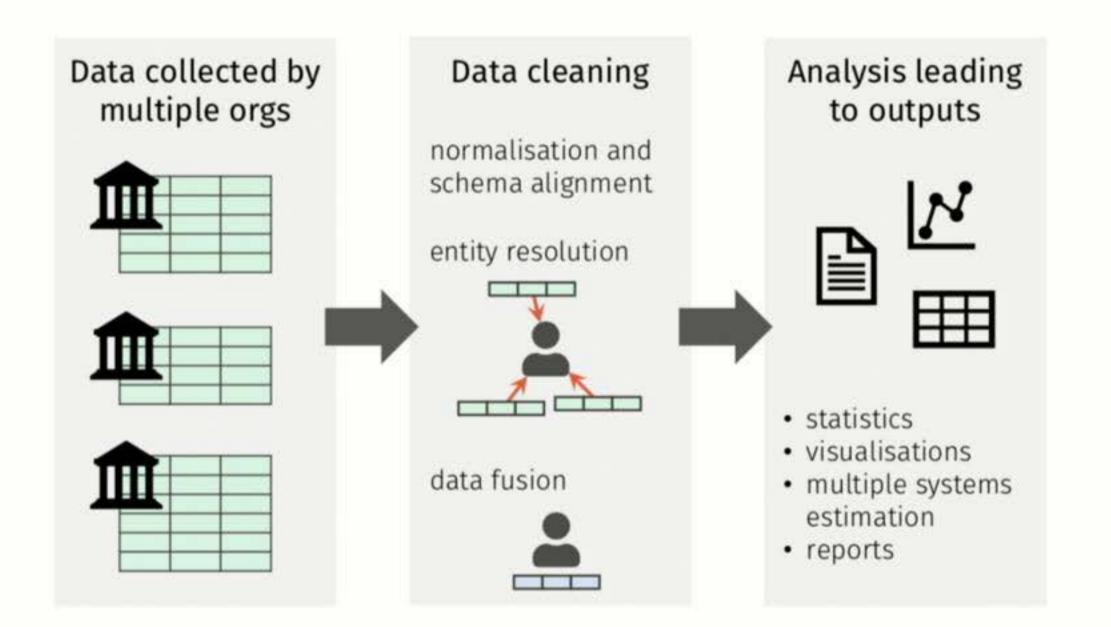
- El Salvador underwent a civil war from 1980 to 1991.
- The United Nations created a Truth Commission (UNTC) to record death casualties/disappearances related to the war by inviting witnesses through newspaper, radio, and television advertisements.
- Human rights groups often depend on accurate estimates and evaluations of the number of documented identifiable deaths for purposes of court ruling, etc.



# PUZNTE DIRECTA LISTA DE VICTIMAS CUYA IDENTIDAD NO SE MANTIZNE EN RESERVA

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ABARCA ABARCA ABARCA	MARIA CRUZ MAURICIO MILTON	WIGLACION HOMICIDIO HOMICIDIO DESAPARIO	0/ 3/88 12/11/80 2/11/80	60100 80118 80100	PH	GN	FFAA	
ABARCA ABARCA ABARCA	NICOLAS ALPASO NICOLAS RUTILIO RICARDO	HOMICIDIO HOMICIDIO LESICHES	0/ 6/86 12/11/80 0/ 0/85 9/ 7/80	40000 80118 42802 90605	PH PH FFAA PARAMT	GM	FFAA	
ABARCA ORELLANA	RUFINO	HCM1C1010	29/ 4/80	42102	PH	PARAMI		
ABARCA ABARCA ABELAR RONGUILLO	TOBIAS TOVIAS ULALIO EDWIN ANTONIO	HOMICIDIO HOMICIDIO	29/ 4/80 22/ 8/82 13/ 1/86 13/ 1/82	100502 20000 60101 43300	FFAA FFAA ESCUAD	FFAA	FFAA	
ABELAR ABELAR	MARIA CRUZ MAURICIO MILTON MICOLAS ALFREDO MICOLAS RUTILIO RICARDO ROSALIMA RUFINO TOBIAS TOVIAS ULALIO EDWIN ANTONIO HERMINO JOSE MARIO ADRIAN ANDRES ANTONIO BENITO BLANCA CARLOS ALFREDO CARMEN ELENA FIDE	HOMICIDIO HOMICIDIO	24/12/80 16/ 5/80 0/ 0/82 10/ 8/83	90205 40901	FFAA PARAMI GN GN	FFAA PARAMI	GM	
ABREGO ABREGO ABREGO ABREGO ABREGO ABREGO CASTRO	ANTONIO BENITO BLANCA CARLOS ALFREDO	HCM1CIDIO HCM1CIDIO DESAPARIC	14/ 8/86 0/ 0/ 0 29/11/80 17/ 4/89	40200 41401 16000	FFAA FFAA			
ABREGO ABREGO ABREGO	CARMEN ELENA FIDE_ FRANCISCO ANTONIO	HOMICIDIO DESAPARIC HOMICIDIO	26/ 3/82 10/ 6/80 12/ 3/84	41902 41501 41902	GH PARAMI	PARAMI		
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ABREGO CASTRO	JOSE ALFONSO JOSE ERMESTO JOSE MARINO DE JESUS	DESAPARIC HOMICIDIO	22/11/80 2/11/89 25/ 2/80	60800 100107	FFM	***		

Extract from Report of the UN Truth Commission of El Salvador (1993)



## Fully Non-parametric ER model

$$\sigma \sim \operatorname{Gamma}[b^0, b^1]$$

$$d \sim \operatorname{Beta}[c^0, c^1]$$

$$\pi \sim \operatorname{PPY}[\sigma, d]$$

$$\lambda_{tr} \mid \pi \sim \operatorname{Categorical}[\pi]$$

$$\mathbf{y}_e \mid G_0 \sim G_0$$

$$H_{ea} \mid \mathbf{y}_{ea} \sim \operatorname{DP}[\beta_a; \Psi_a(\mathbf{y}_{ea})]$$

$$\theta_{ta} \sim \operatorname{Beta}[\alpha_a^0, \alpha_a^1]$$

$$\zeta_{tra} \mid \mathbf{y}_{\lambda_{tr}a}, \lambda_{tr} = \max_{\mathbf{v} \in V_a} e^{-\operatorname{dist}_a(\mathbf{y}_{\lambda_{tr}a}, \mathbf{v})}$$

$$z_{tra} \mid \theta_{ta}, \zeta_{tra} \sim \operatorname{Bernoulli}[\theta_{ta}\zeta_{tra}]$$

$$x_{tra} \mid z_{tra}, \mathbf{y}_{\lambda_{tr}a}, \lambda_{tr} \sim (1 - z_{tra})\delta[\mathbf{y}_{\lambda_{tr}a}] + z_{tra}H_{ea}$$

where  $g_0 \mathbf{y} = \prod_a \phi_a(\mathbf{v})$  and  $\psi_a(\mathbf{v}|\mathbf{y}) \propto \phi_a(\mathbf{v})e^{-\operatorname{dist}_a(\mathbf{y},\mathbf{v})}$ .

# PUENTE DIRECTA LISTA DE VICTIMAS CUYA IDENTIDAD NO SE MANTIZNE EN RESERVA

APELL IDOS	NO SERVICES	HECK)	FECH	LUGAR	RESP1	HE22	RESP3	RESPA
		AFF101215	0/ 6/31	80101	FFAA	FFAA		
ABARCA PINEDA	JULIO CESAR	010:31MCH	10/ 7/34	60000 42008	FFAA	PH	PARAMI	GN
ABARCA	LUIS LUIS MARIA CRUZ	HCM1C:D10	14/ 5/80 20/ 1/82 26/12/90	100504	FFAA	FFAA		
ABARCA	MADRICIO	DESAPARIC HOMIC:DIO HOMIC:DIO YIOLACION HOMIC:DIO DESAPARIC HOMIC:DIO HOMIC:DIO HOMIC:DIO HOMIC:DIO HOMIC:DIO	26/12/90 0/ 3/88 12/11/80	60100 80118	PH	GN	FFAA	
	MILTON MICOLAS ALFREDO	DESAPARIC	2/11/80 0/ 6/86 12/11/80	80100 40000	FHLH	GN	FFAA	
ABARCA ABARCA	RICARDO	HEMICIDIO	12/11/80 0/ 0/85 9/ 7/80	80118 42802 90605	PH FFAA PARAMI	••	*****	
ABARCA ABELAR ABELAR ABELAR	MILTON MICOLAS ALFREDO MICOLAS RUTILIO RICARDO ROSALINA RUFINO TOBIAS TOVIAS ULALIO EDWIN ANTONIO HERMINO JOSE MARIO ADRIAN ANDRES ANTONIO BLANCA	HCM1C1010	29/ 4/80	42102	PH	PARAM1		
ABARCA	TOVIAS	HCH1CIDIO	29/ 4/80 22/ 8/82 13/ 1/86	100502	FFAA	FFAA	FFAA	
ABELAR RONGUILLO	EDWIN ANTONIO	HCM1CIDIO	13/ 1/82	60101 43300	FFAA			
ABELAR	JOSE MARIO	HCM1CIDIO	24/12/80 16/ 5/80	40302	PARAMI	FFAA	GM	
ABREGO	ANDRES	HCM1C1010	10/ 8/83	40302 90205 40901 40200	GN FFAA	PARAMI		
ABREGO ABREGO	SENITO	HCM1CIDIO	0/ 0/ 0	41401 16000	PH			
ABREGO CASTRO	CARLUS METMEDO	DESAPARIC TORTURA HOMICIDIO	29/11/80 17/ 4/89	41902	FFM			
ABREGO ABREGO	CARMEN ELEXA	DESAPARIC HOMICIDIO	26/ 3/82 10/ 6/80 12/ 3/84	41501 41902	GN PARAMI	PARAMI		
ABREGO	FRANCISCO ANTONIO	HOMICIDIO	22/11/80	0	100 C			
	GUILLERMO ISRAEL	DESAPARIC HOMICIDIO	0/ 5/84	40906 71525	FFAA	FFAA		
ABREGO ABREGO	JOSE	HCMICIDIO	11/11/80	40906	ESCUAD			
ABREGO CASTRO	JOSE ALFONSO JOSE ERNESTO JOSE MARINO DE JESUS	DESAPARIC HOMICIDIO	2/11/80 2/11/89	60800 100107	FFAA			
ARPECO MAVADOO	TOPE WAKING DE SESOS	COTTONES	25/ 2/80	100107	4.4.00	- C	DADAMT	

Extract from Report of the UN Truth Commission of El Salvador (1993)

## Fully Non-parametric ER model

$$\sigma \sim \operatorname{Gamma}[b^0, b^1]$$

$$d \sim \operatorname{Beta}[c^0, c^1]$$

$$\pi \sim \operatorname{PPY}[\sigma, d]$$

$$\lambda_{tr} \mid \pi \sim \operatorname{Categorical}[\pi]$$

$$\mathbf{y}_e \mid G_0 \sim G_0$$

$$H_{ea} \mid \mathbf{y}_{ea} \sim \operatorname{DP}[\beta_a; \Psi_a(\mathbf{y}_{ea})]$$

$$\theta_{ta} \sim \operatorname{Beta}[\alpha_a^0, \alpha_a^1]$$

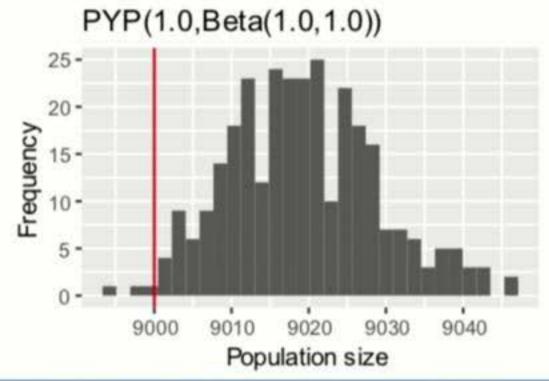
$$\zeta_{tra} \mid \mathbf{y}_{\lambda_{tr}a}, \lambda_{tr} = \max_{\mathbf{v} \in V_a} e^{-\operatorname{dist}_a(\mathbf{y}_{\lambda_{tr}a}, \mathbf{v})}$$

$$z_{tra} \mid \theta_{ta}, \zeta_{tra} \sim \operatorname{Bernoulli}[\theta_{ta}\zeta_{tra}]$$

$$x_{tra} \mid z_{tra}, \mathbf{y}_{\lambda_{tr}a}, \lambda_{tr} \sim (1 - z_{tra})\delta[\mathbf{y}_{\lambda_{tr}a}] + z_{tra}H_{ea}$$

where  $g_0 \mathbf{y} = \prod_a \phi_a(v)$  and  $\psi_a(v|y) \propto \phi_a(v)e^{-\operatorname{dist}_a(y,v)}$ .

## RLdata10000



Prior type	% rel. error # entities	Precision	Recall
PYP	0.2%	0.97	0.98
DP	-50%	0.07	1.00
Uniform	-47%	0.10	0.99
Coupon	-15%	0.50	0.99

## Results

### Table: Comparison of PYP, DP and Uniform prior on UNTC.

Prior	а	Ь	θ	$\sigma$	Precision	Recall	Posterior mean	SE	Runtime (sec)
			1.7272	0.9890	0.900	0.153	725.45	1.27	892.17
PYP	1	99	2.5663	0.9885	0.900	0.153	725.58	1.64	894.91
			4.6017	0.9875	0.900	0.153	728.21	1.27	803.36
			1		0.770	0.797	678.237	1.38	997.8
DP	1	99	2	-	0.797	0.797	680.08	1.79	1054.2
			3		0.793	0.780	682.18	1.74	1042.2
11-:6	1	73.5	5		0.867	0.661	692.47	2.58	3490.09
Uniform	1	99	-	-	0.826	0.644	688.84	2.18	3280.19

## Example of False Positive Error

Table: Our model currently clusters these records to the same latent entity. But according to the hand matched labels, there are actually two latent entities here. We believe that this hand-matched label could be easily labeled as match or not-match depending on the hand-matcher.

Firstname	Lastname	Year	Month	Day	Department	Municipality
CARMEN	ALFARO	1982	3	21	7	716
JOSE	ALFARO GAMES	1980	3	22	7	716
CARMEN	ALFARO GAMES	1980	3	22	7	716

### **UNTC** dataset

Record	Given name	Family name	Year	Month	Day	Municipality
1.	JOSE	FLORES	1981	1	29	A
2.	JOSE	FLORES	1981	2	NA	A
3.	JOSE	FLORES	1981	3	20	A
4.	JULIAN ANDRES	RAMOS ROJAS	1986	8	5	В
5.	JILIAM	RMAOS	1986	8	5	В

We utilize a similar type of framework to Marchant et. al (2019), however we consider a set of more flexible priors on the linkage structure and a different type of string metrics for the hispanic names.

## Theoretical Limits for Entity Resolution

Are there theoretical limits for entity resolution? Yes!

Two very different approaches:

- 1 Johndrow, Lum, and Dunson, Biometrika, 2018.
  - The authors show that that for p features or when the number of entities is small compared to the number of records that entity resolution is "effectively impossible."
- RCS, Barnes, Neiswanger (2017), AIStats, http://proceedings.mlr.press/v54/.
  - We derive performance bounds (lower bounds) using the KL divergence on when a latent entity is mis-classified, showing when the bounds are tight.

Thank you!

Questions?

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https://github.com/resteorts/record-linkage-tutorial