

Enabling Multi-scale Science: Mathematical and Computational Modeling

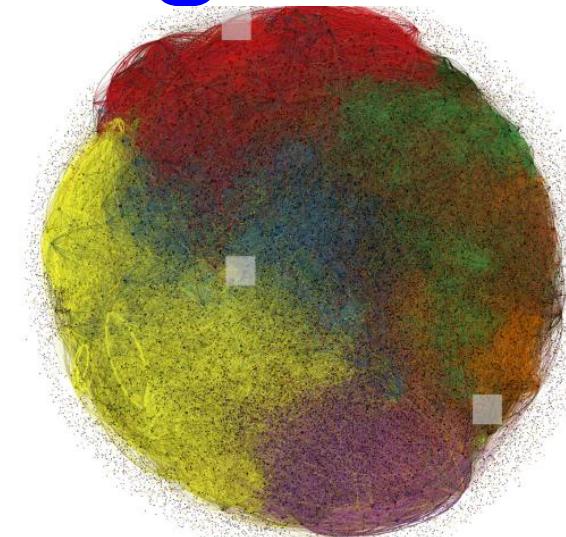
Roberto M. Cesar-Jr

IME – USP

<http://www.ime.usp.br/~cesar/>

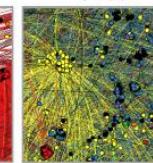
eScience-USP

FAPESP – CNPq - Capes

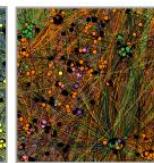


Major knowledge areas:

- Agricultural Sciences
- Humanities
- Engineering



● Biological Sciences
● Applied Social Sciences
● Linguistics, Letters and Arts
● More than one major area



● Exact and Earth Sciences
● Health Sciences
● More than one major area



Summary

- Which “scale”?
- Multi-scale HOWTO
- Concluding remarks?

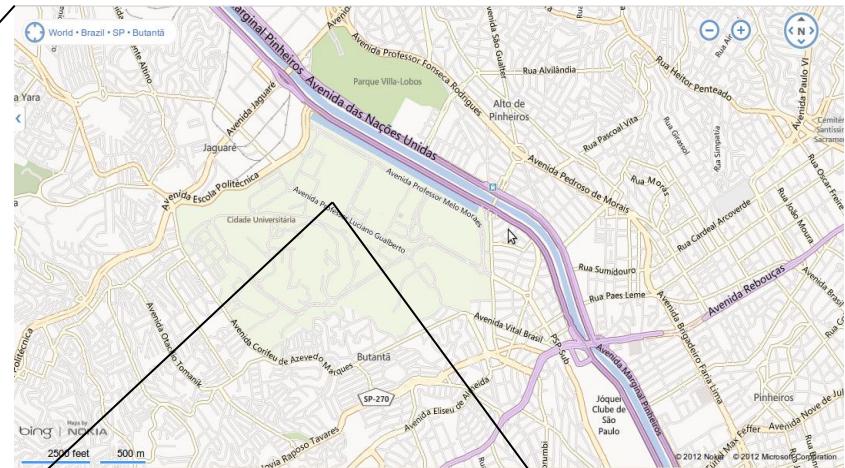
Which “scale”?

Which “scale”...

...are we talking about?

- Spatial
- Temporal
- Conceptual
- ?

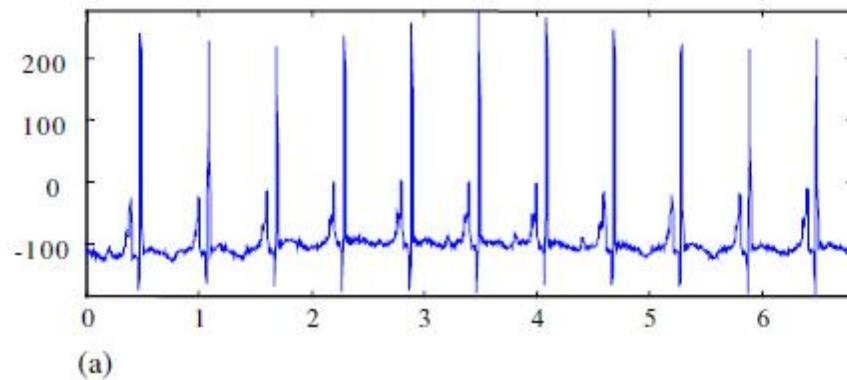
Which “scale”...



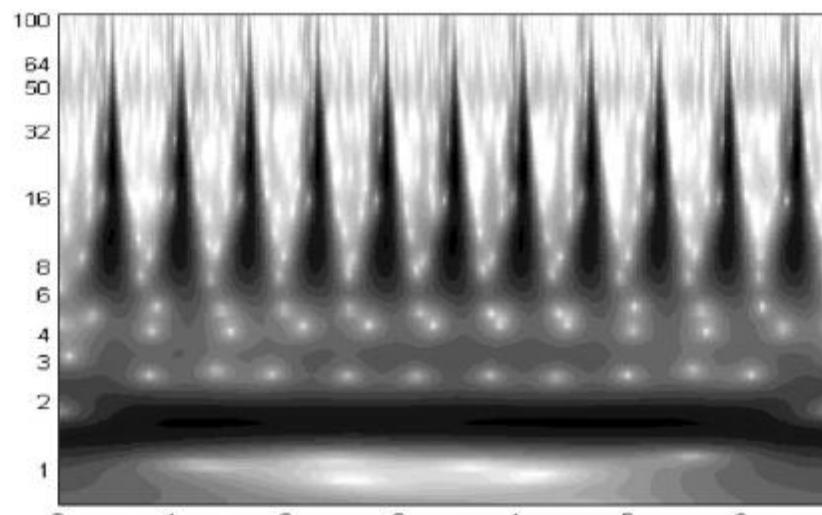
Spatial scales



Which “scale”...



(a)



(b)

Temporal scales

INSTITUTE OF PHYSICS PUBLISHING
Physiol. Meas. 26 (2005) R155-R199

PHYSIOLOGICAL MEASUREMENT
doi:10.1088/0967-3334/26/5/R01

TOPICAL REVIEW

Wavelet transforms and the ECG: a review

Paul S Addison

CardioDigital Ltd, Elvingston Science Centre, East Lothian, EH33 1EH, UK
E-mail: p.addison@cardiodigital.com



Universidade de São Paulo
BRASIL



Central dogma of biology

Data-intensive knowledge discovery and systems biology: Conceptual scales

Replication

Transcription

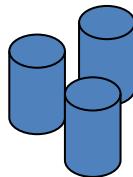
Translation



DNA



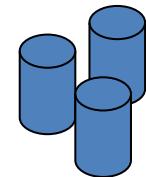
Genomics



mRNA



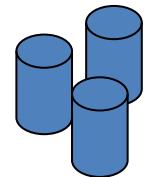
Transcriptomics



Proteins



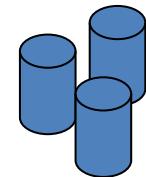
Proteomics



Metabolites



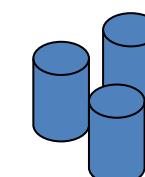
Metabolomics



Organisms

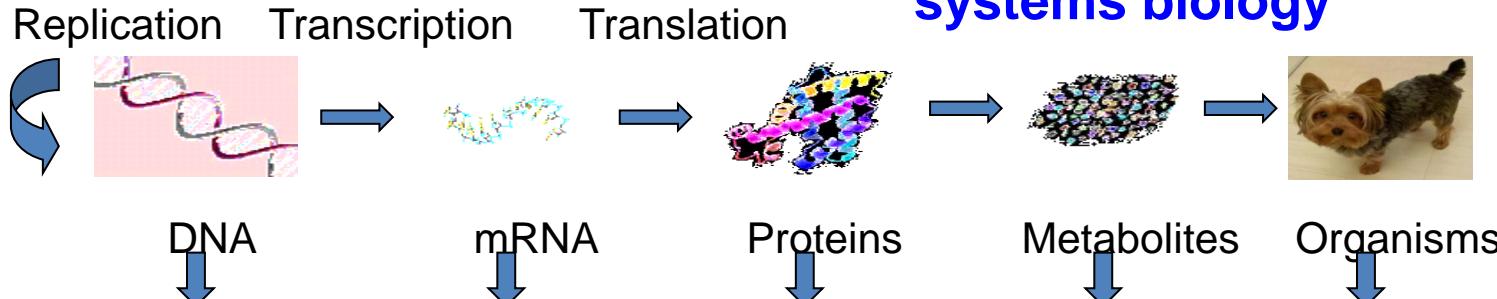


Various
analysis



Heterogeneous, complex, distributed databases

Data-intensive knowledge discovery and systems biology



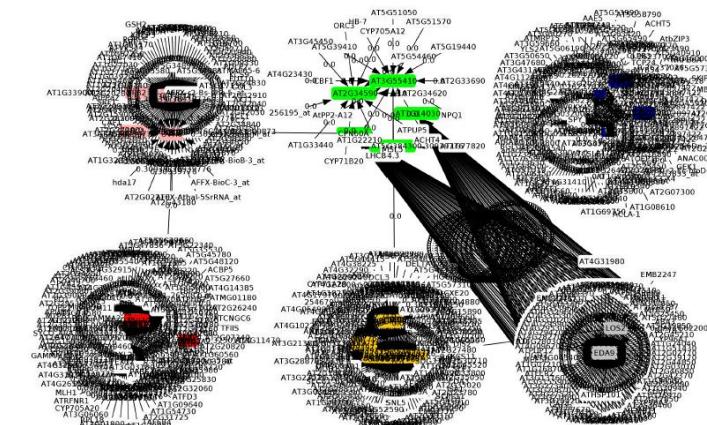
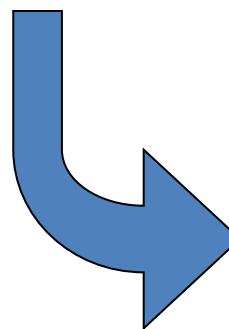
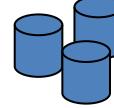
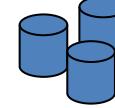
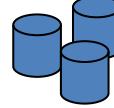
Genomics

Transcriptomics

Proteomics

Metabolomics

Organisms



Second order conceptual scales



Multi-scale HOWTO

HOWTO

- Problems with or without inherent scales
- Mathematical approaches available (continuous, discrete, multidimensional):
 - Wavelets
 - Pyramids and Resolution
 - Graphs
 -
- Computational methods and structures

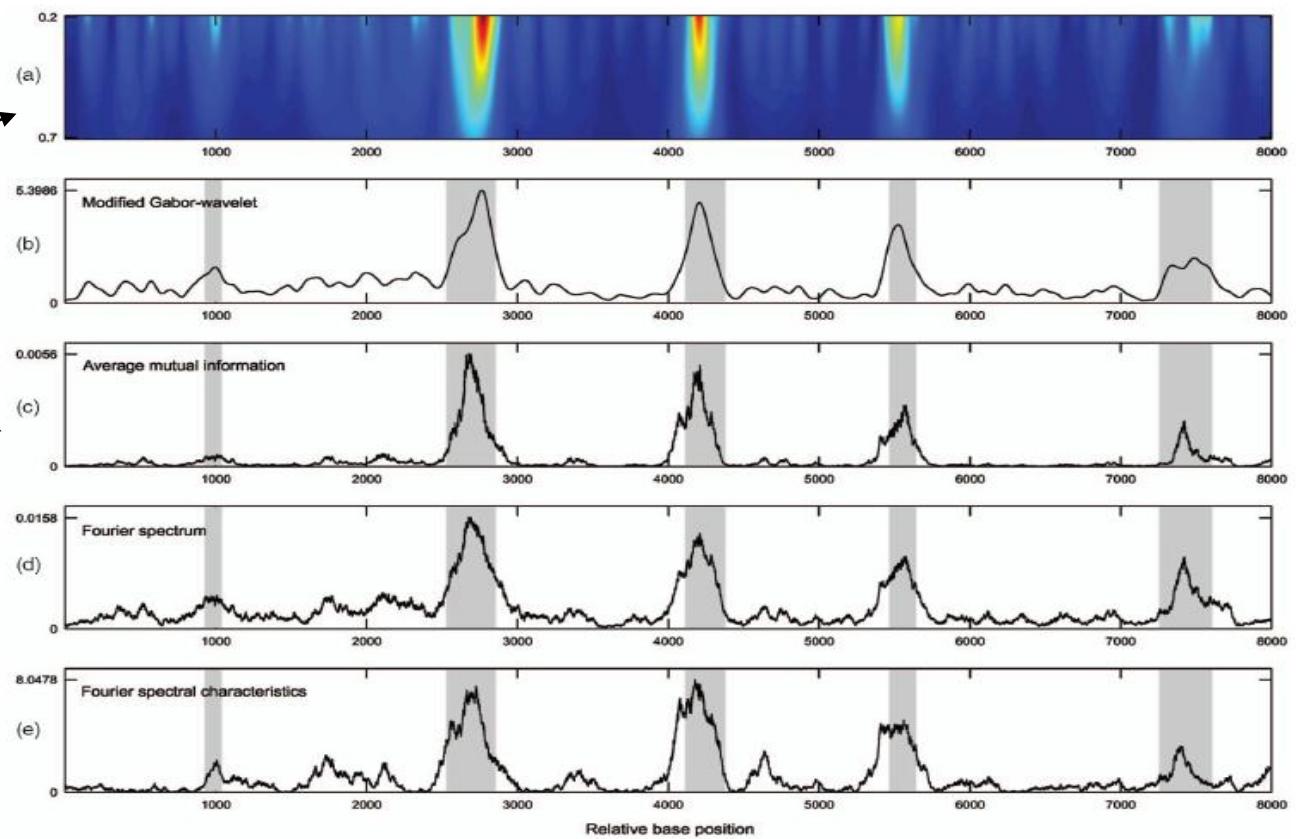
HOWTO



IEEE/ACM TRANSACTIONS ON COMPUTATIONAL BIOLOGY AND BIOINFORMATICS, VOL. 5, NO. 2, APRIL-JUNE 2008

Information:

- coding
- unfolding
- folding



198 IEEE/ACM TRANSACTIONS ON COMPUTATIONAL BIOLOGY AND BIOINFORMATICS, VOL. 5, NO. 2, APRIL-JUNE 2008

Identification of Protein Coding Regions Using the Modified Gabor-Wavelet Transform

Jesús P. Mena-Chalco, Helaine Carrer, Yossi Zana, and Roberto M. Cesar Jr.

© Roberto.Cesar@vision.ime.usp.br

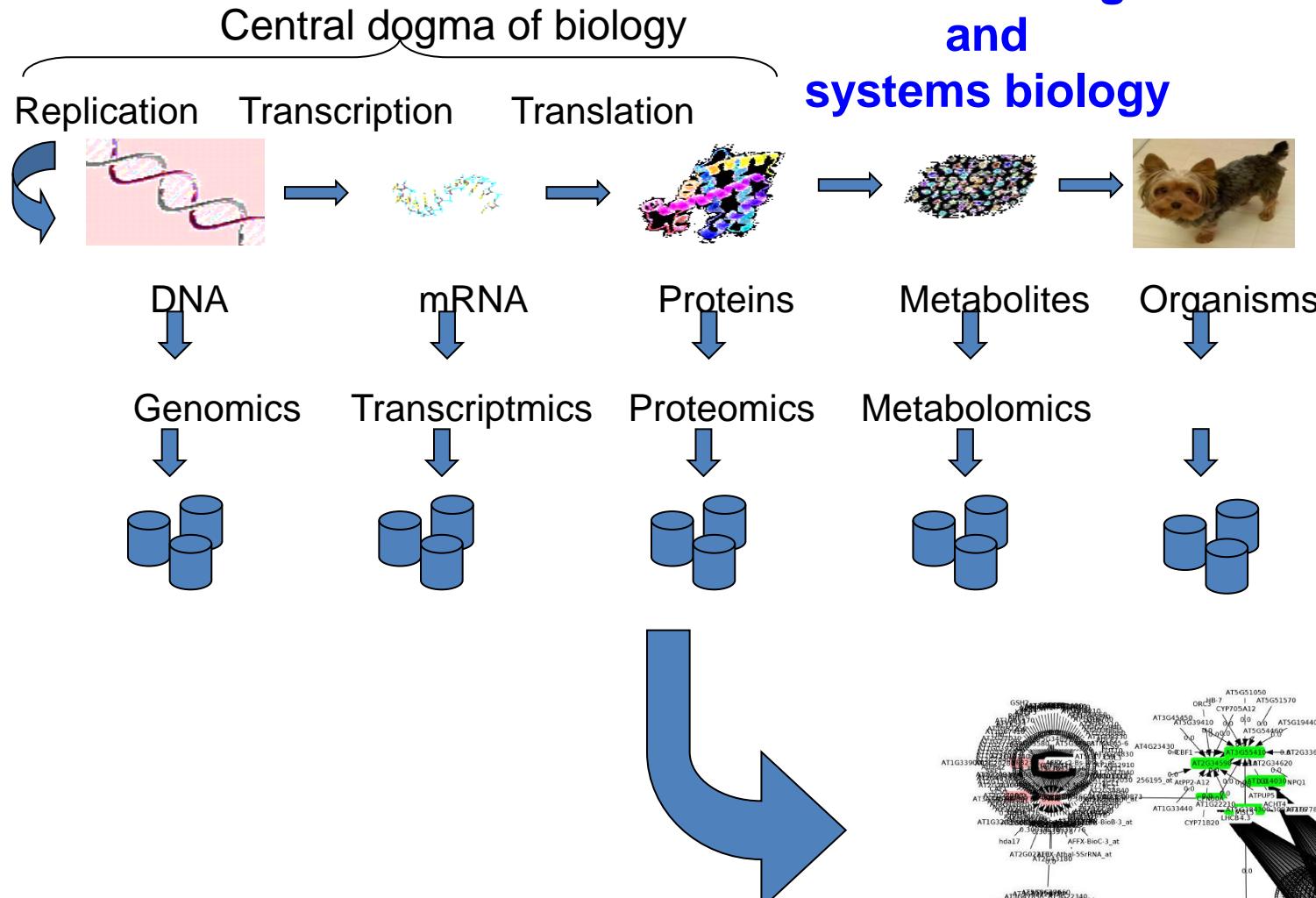


Universidade de São Paulo
BRASIL



HOWTO

Data-intensive knowledge discovery and systems biology



HOWTO

Expression of gene i at time t : $x_i[t] \in \{-1, 0, +1\}$

State of the regulatory network at time t :

$$x[t] = \begin{bmatrix} x_1[t] \\ x_2[t] \\ \vdots \\ \vdots \\ x_n[t] \end{bmatrix}$$

Network dynamics: $x[t+1] = \phi(x[t])$

HOWTO

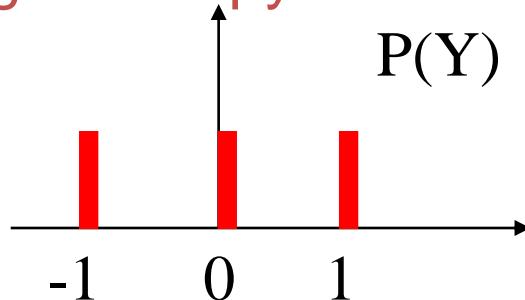
Entropy

$$H(Y) = - \sum_{y \in \{-1, 0, 1\}} P(y) \log P(y)$$

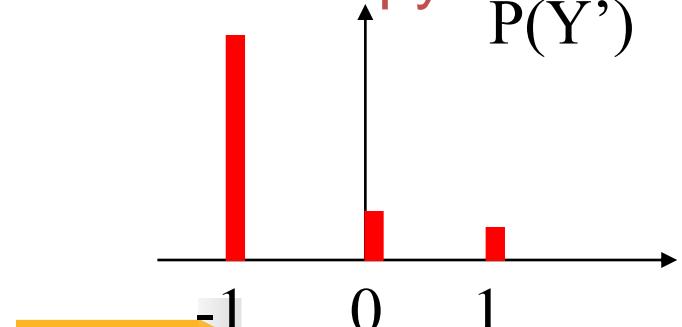
Mean conditional entropy

$$E[H(Y | X)] = - \sum P(X) \sum P(Y | X) \cdot \log(P(Y | X))$$

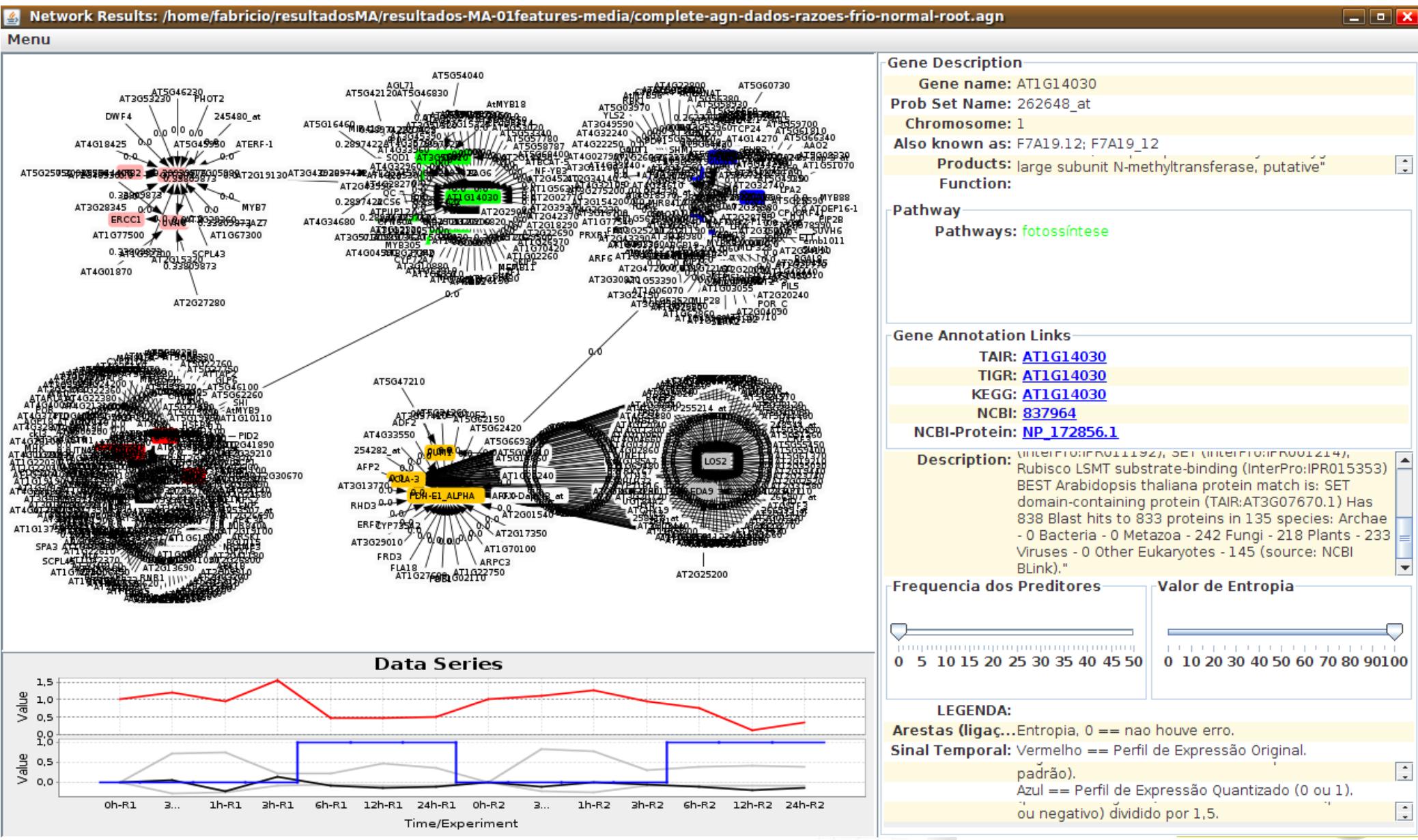
High Entropy



Low Entropy

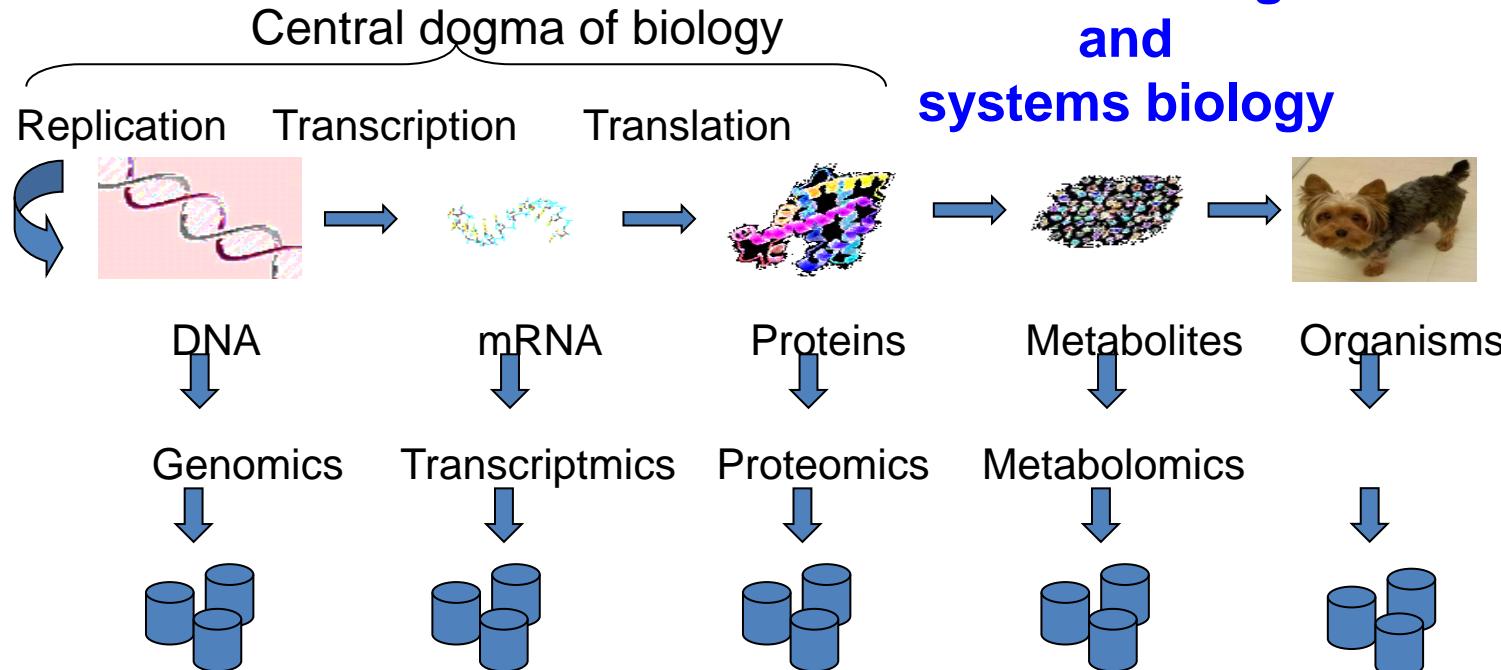


HOWTO

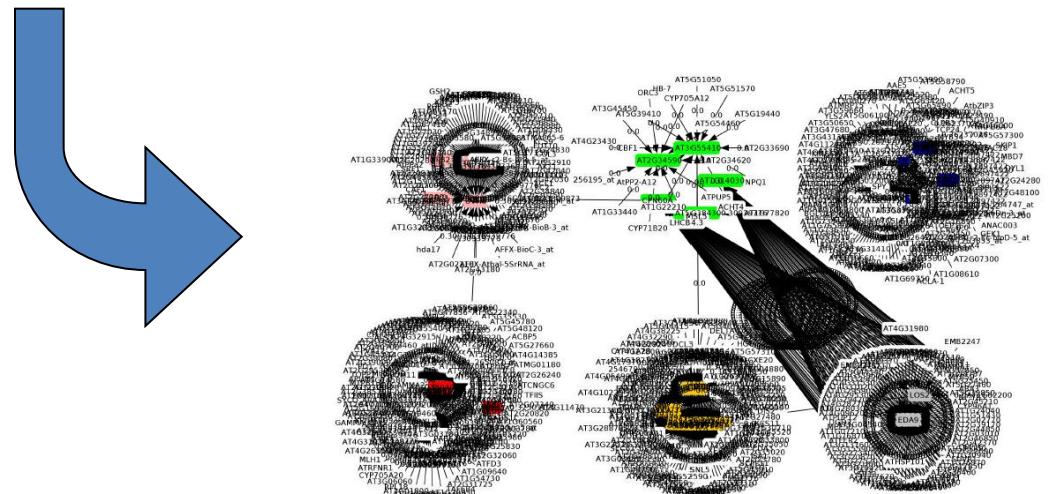


HOWTO

Data-intensive knowledge discovery and systems biology



Mappings between second order conceptual scales



Concluding remarks

HOWTO

- Different “types” of scales
- Problems with inherent scales
- Unfolding and folding the scales
- Mathematical models
- Computational models and data-structures
- Software

Multi-scale for eScience Approaches

- Multi-scale as a way to cope with complexity
- Multiple scales for exploratory data analysis, browsing data, grasping initial understanding,...
- Data integration: mathematical and data models
- Network matching, searching, comparison, motifs