



UNIVERSITY OF OREGON

# PartialGC: A server-aided system for saving GC state

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Research & Information Security  
Laboratory

February 21, 2014



## Privacy Preserving Data Analysis



## Privacy Preserving Data Analysis

Data  
Initialization



## Privacy Preserving Data Analysis



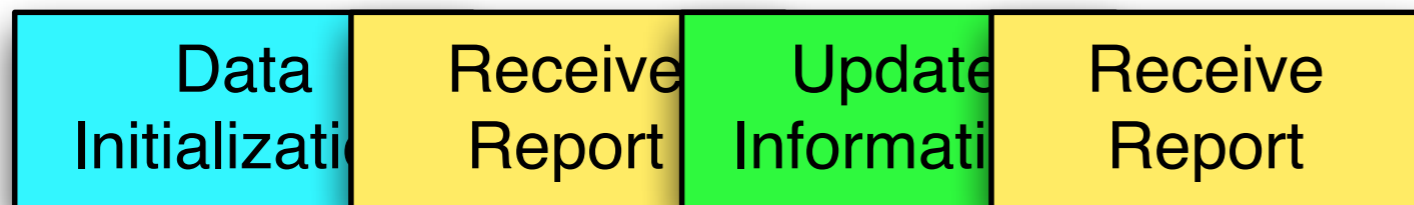


## Privacy Preserving Data Analysis





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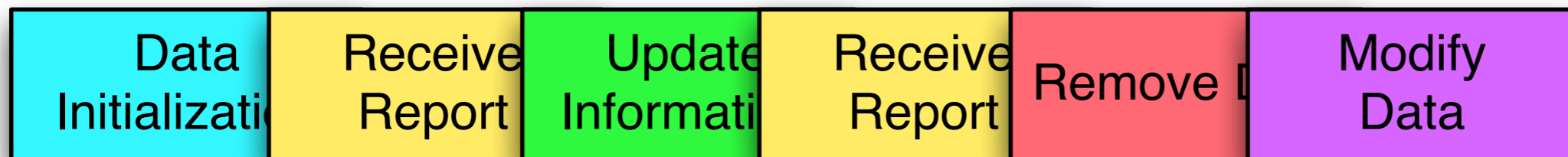


## Privacy Preserving Data Analysis





## Privacy Preserving Data Analysis







## Privacy Preserving Data Analysis



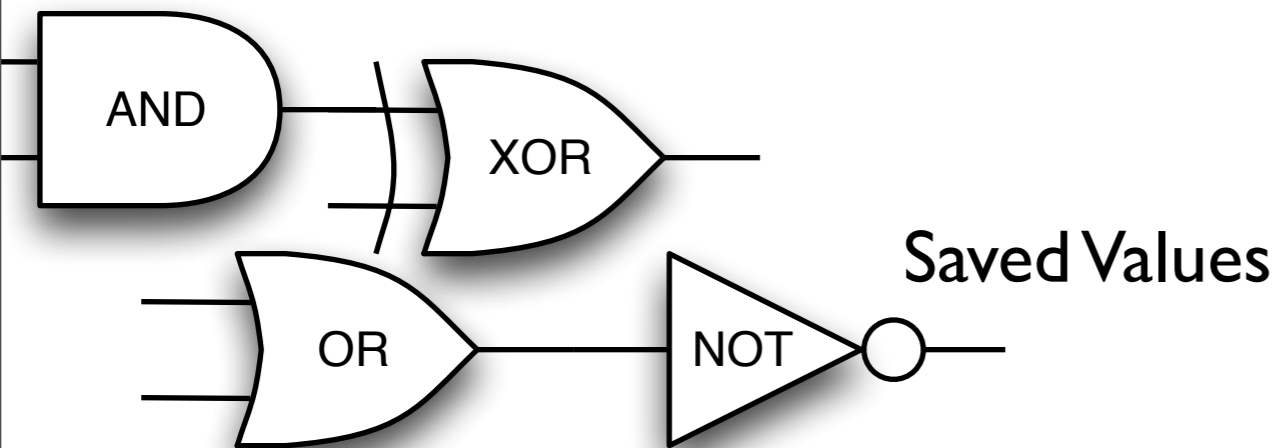
# Overall Idea:



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Garbled Circuit 1

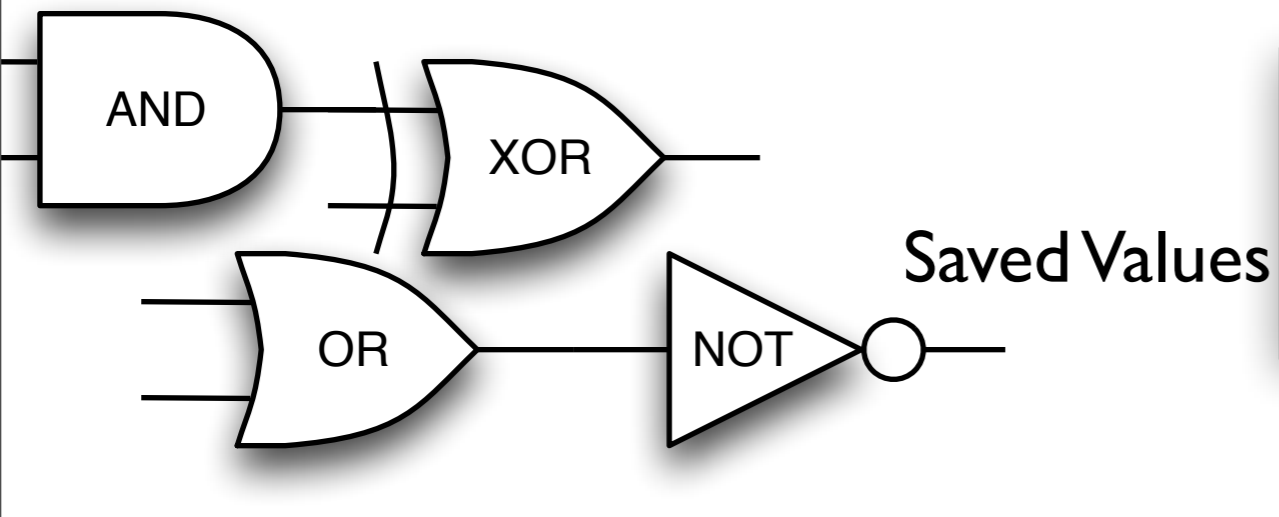


# Overall Idea:



## Transformation Protocol

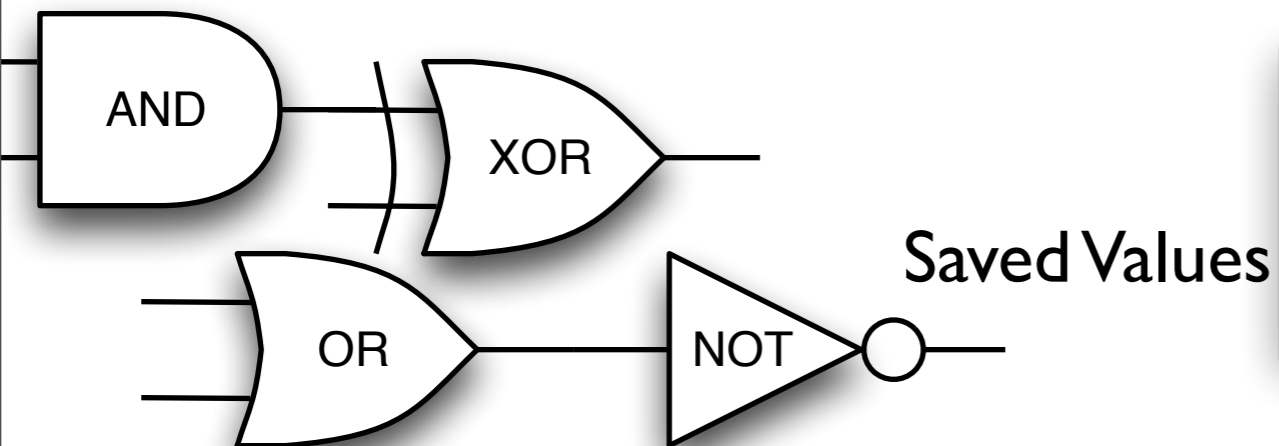
Garbled Circuit 1



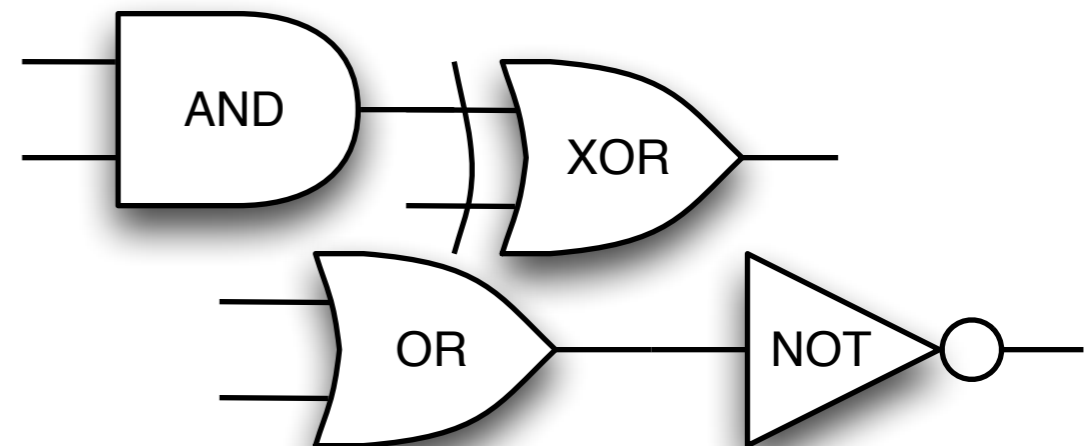
# Overall Idea:

## Transformation Protocol

Garbled Circuit 1



Garbled Circuit 2



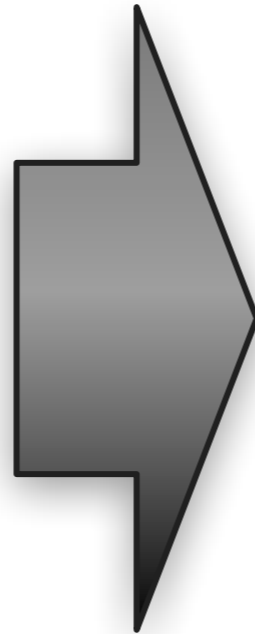
- Transformation
- Checking Transformation
- Server Aided Protocol
- Results

# Transforming Wires

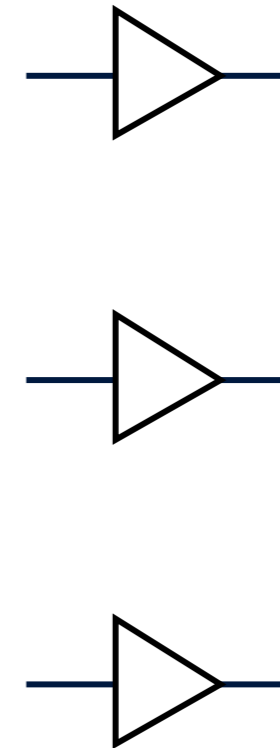
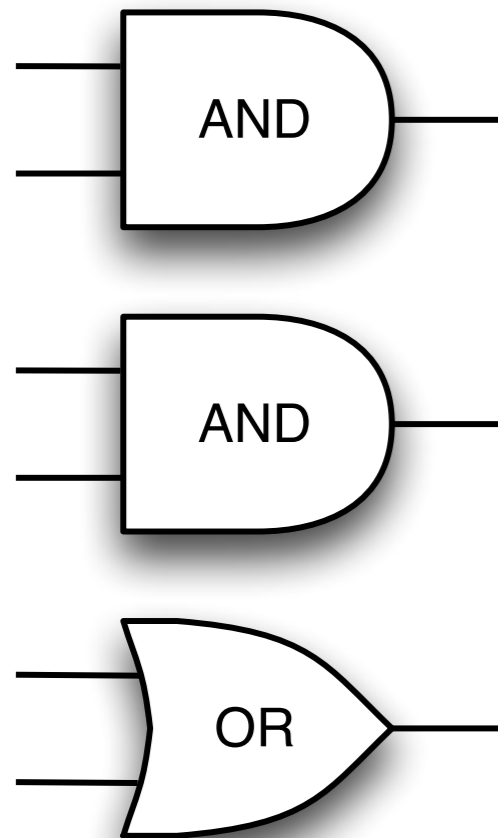


- Generator creates garbled gates that transform the wires that work in one garbled circuit to wires that work in another garbled circuit.

Transformation  
Protocol



# Transformation Details

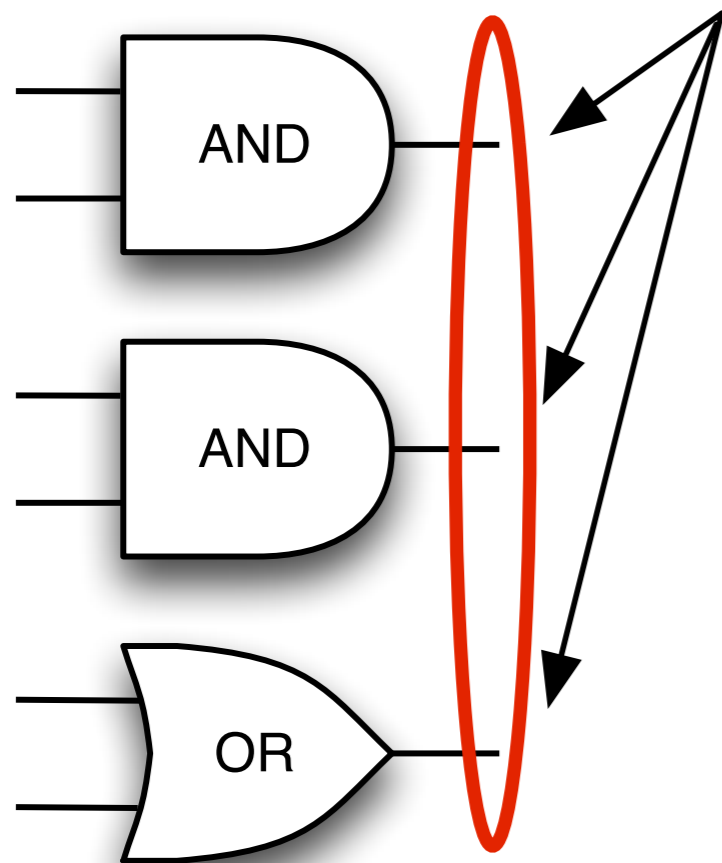


\* = once per circuit

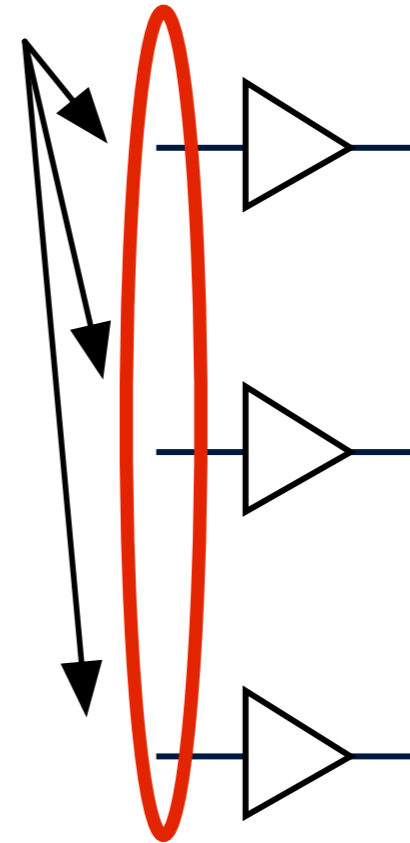


# Transformation Details

Encrypted Output Wires

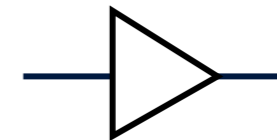
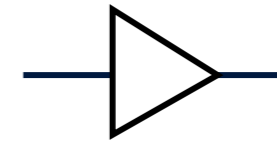
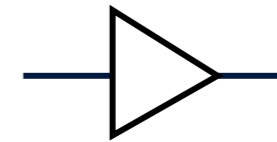
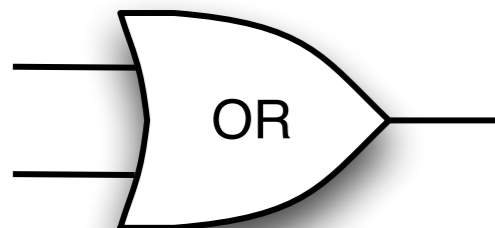
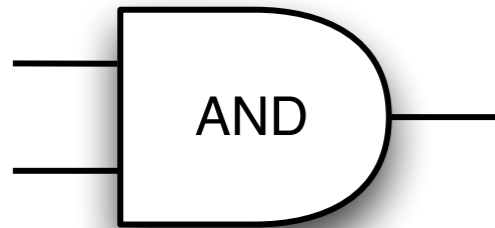
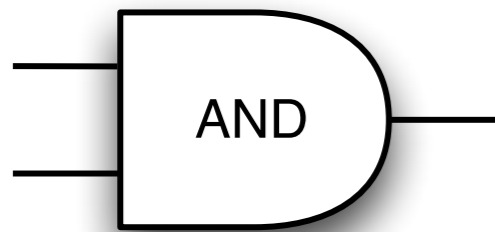


Encrypted Input Wires



\* = once per circuit

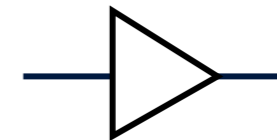
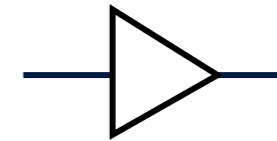
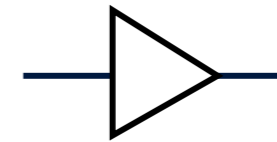
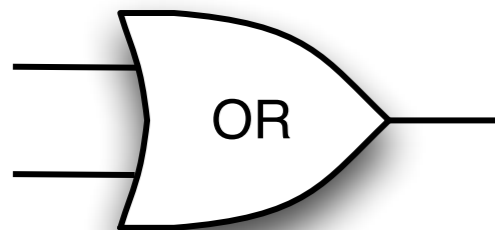
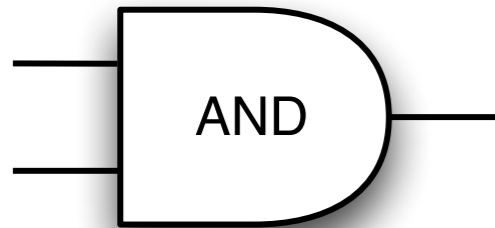
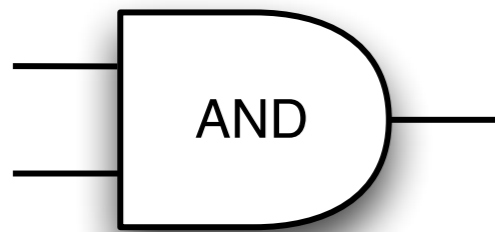
# Transformation Details



\* = once per circuit

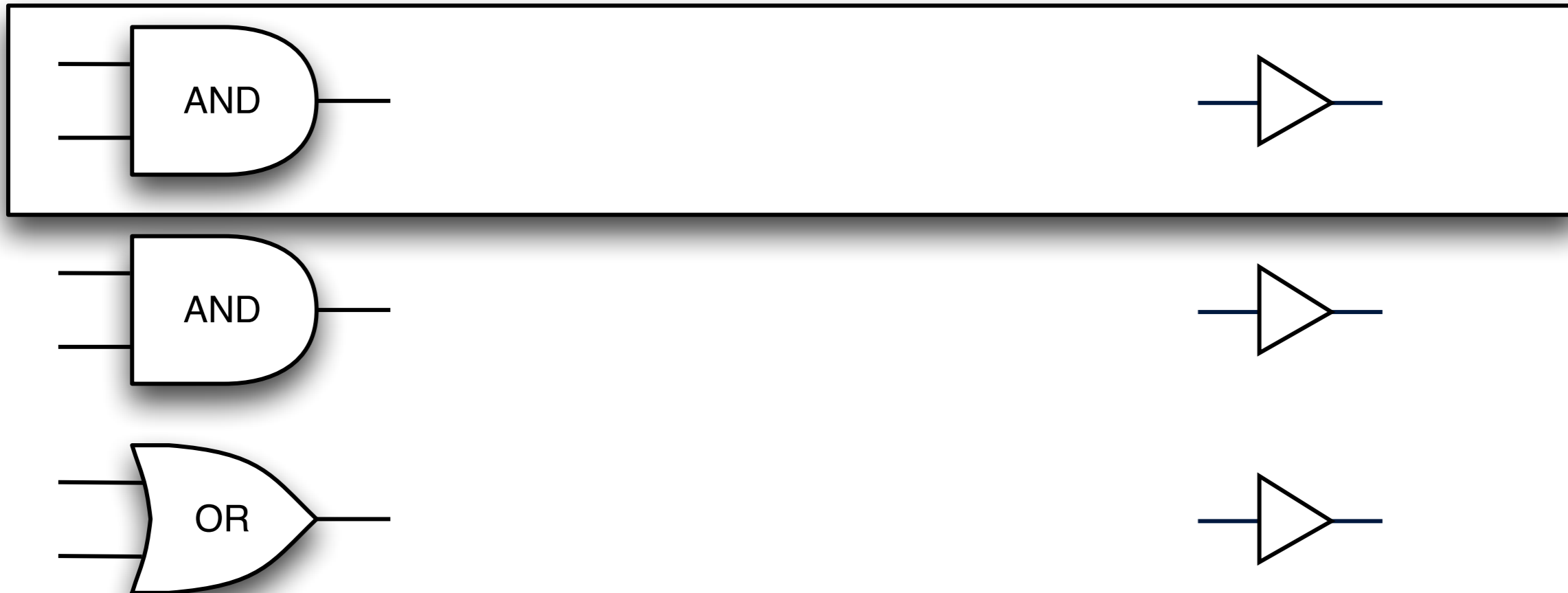
# Transformation Details

## Generator



\* = once per circuit

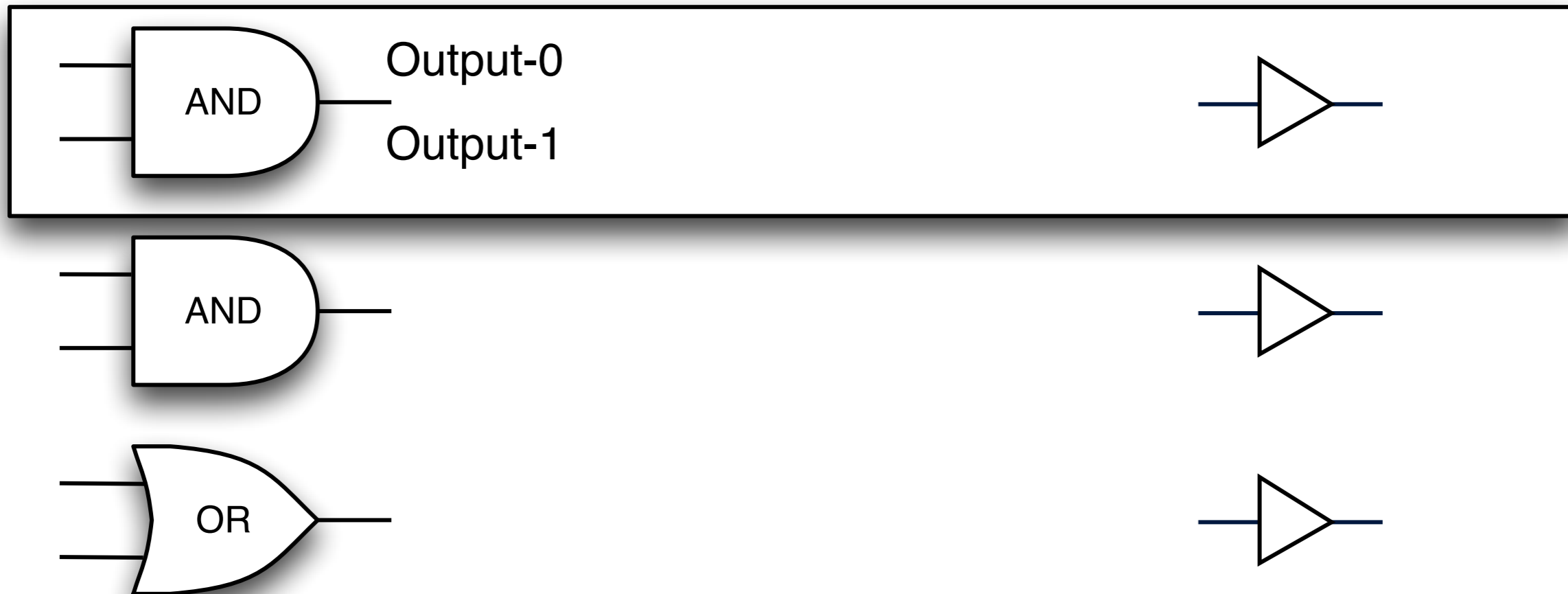
## Generator



\* = once per circuit

# Transformation Details

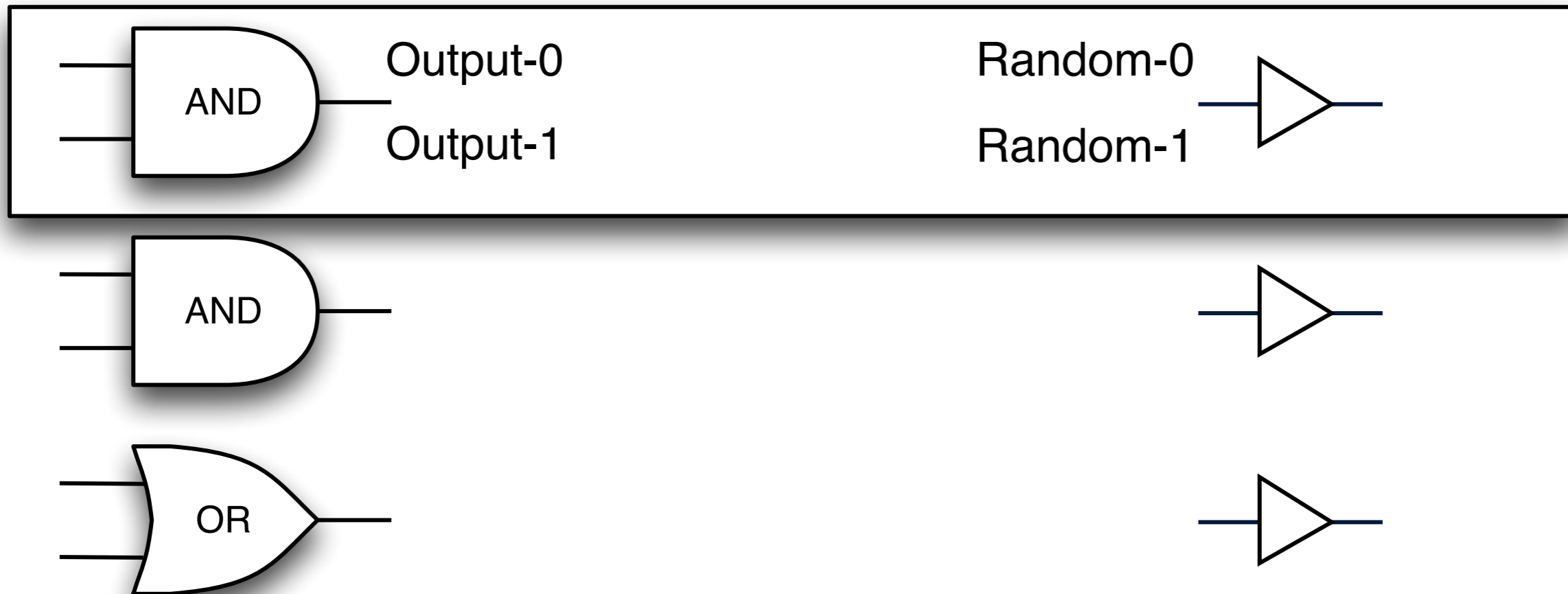
## Generator



\* = once per circuit

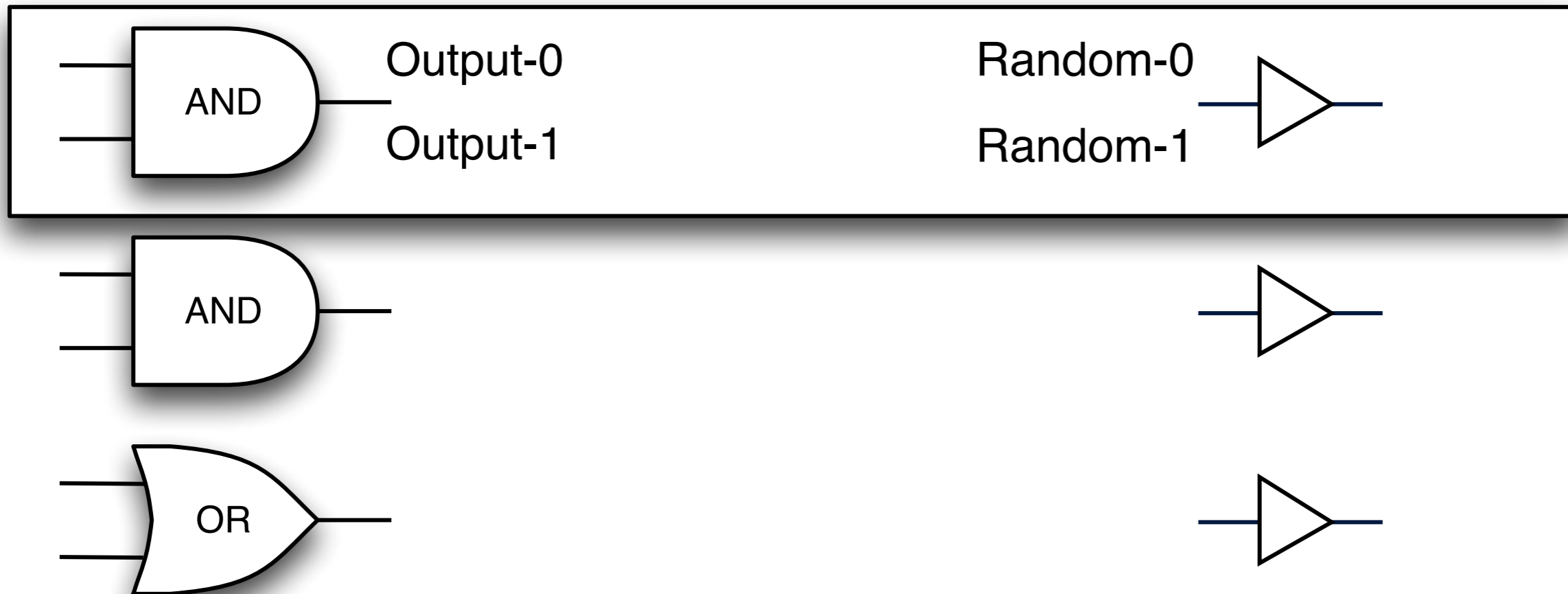
# Transformation Details

## Generator



\* = once per circuit

## Generator



nonce = PRNG.rand() \*

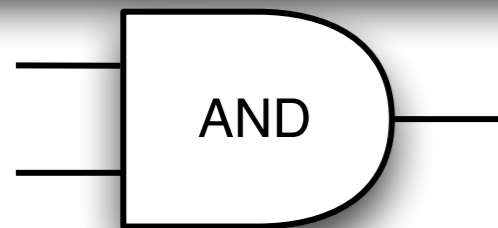
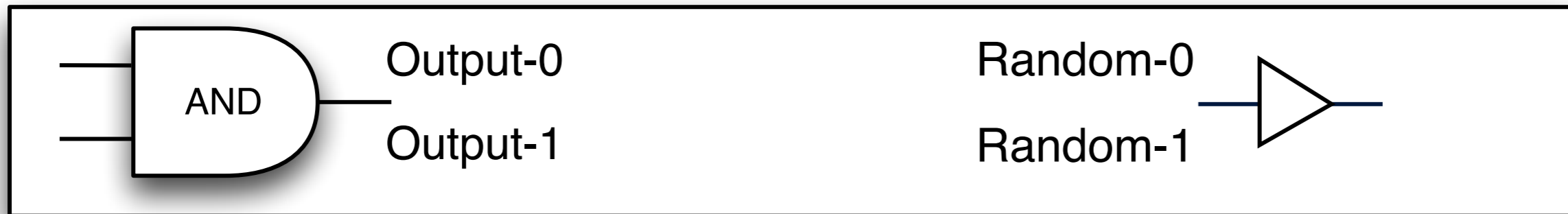
Transform-0 = hash(Output-0  $\oplus$  nonce)  $\oplus$  Random-0

Transform-1 = hash(Output-1  $\oplus$  nonce)  $\oplus$  Random-1

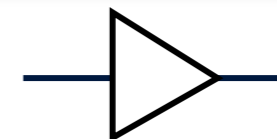
\* = once per circuit

# Transformation Details

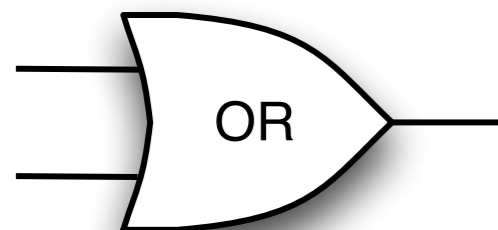
## Generator



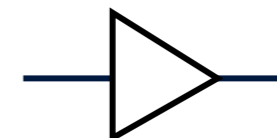
Send To Evaluator



Transform-0



Transform-1



nonce \*

nonce = PRNG.rand() \*

Transform-0 = hash(Output-0  $\oplus$  nonce)  $\oplus$  Random-0

Transform-1 = hash(Output-1  $\oplus$  nonce)  $\oplus$  Random-1

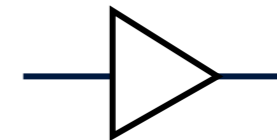
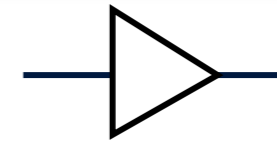
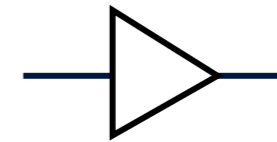
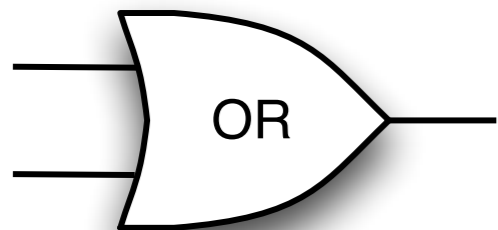
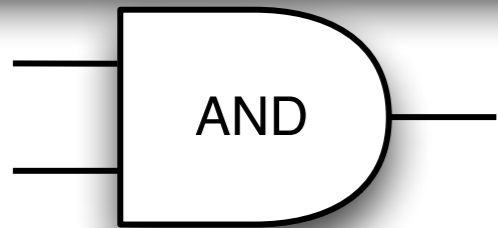
\* = once per circuit



# Transformation Details

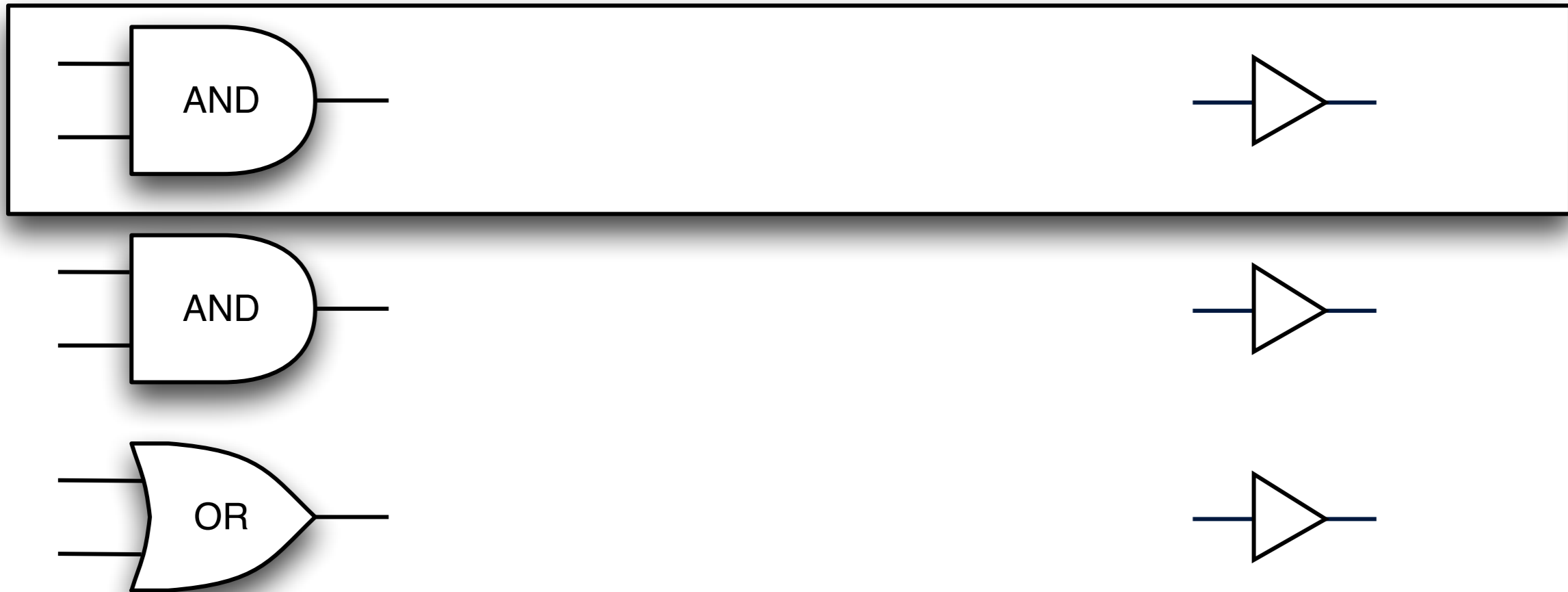


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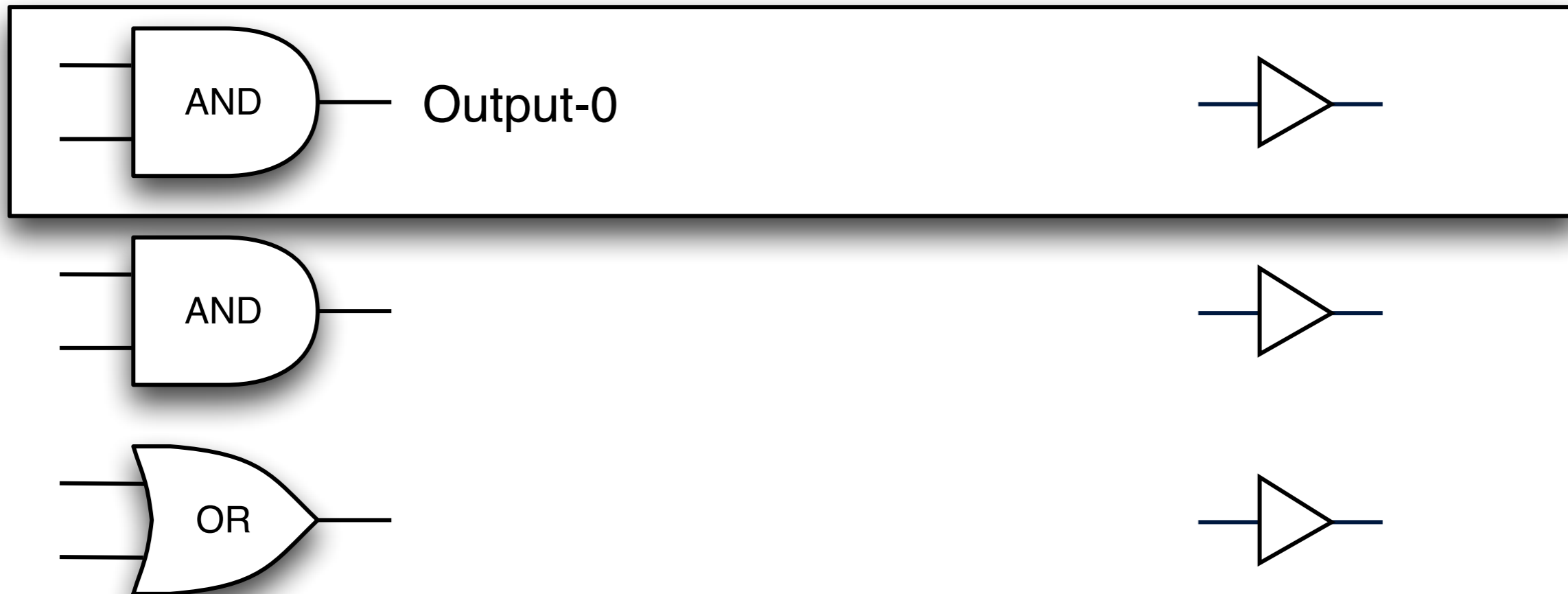
\* = once per circuit

## Evaluator



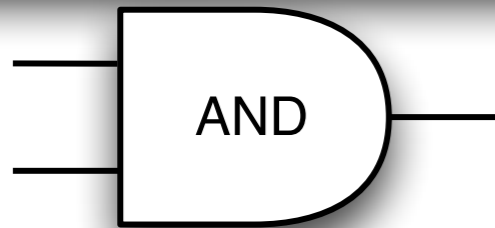
\* = once per circuit

## Evaluator



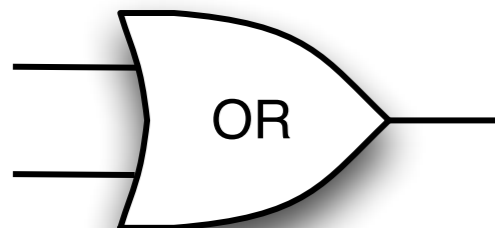
\* = once per circuit

## Evaluator

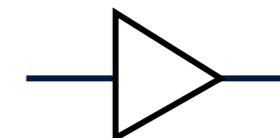
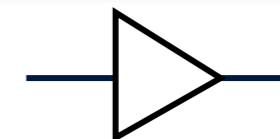


nonce \*

Transform-0

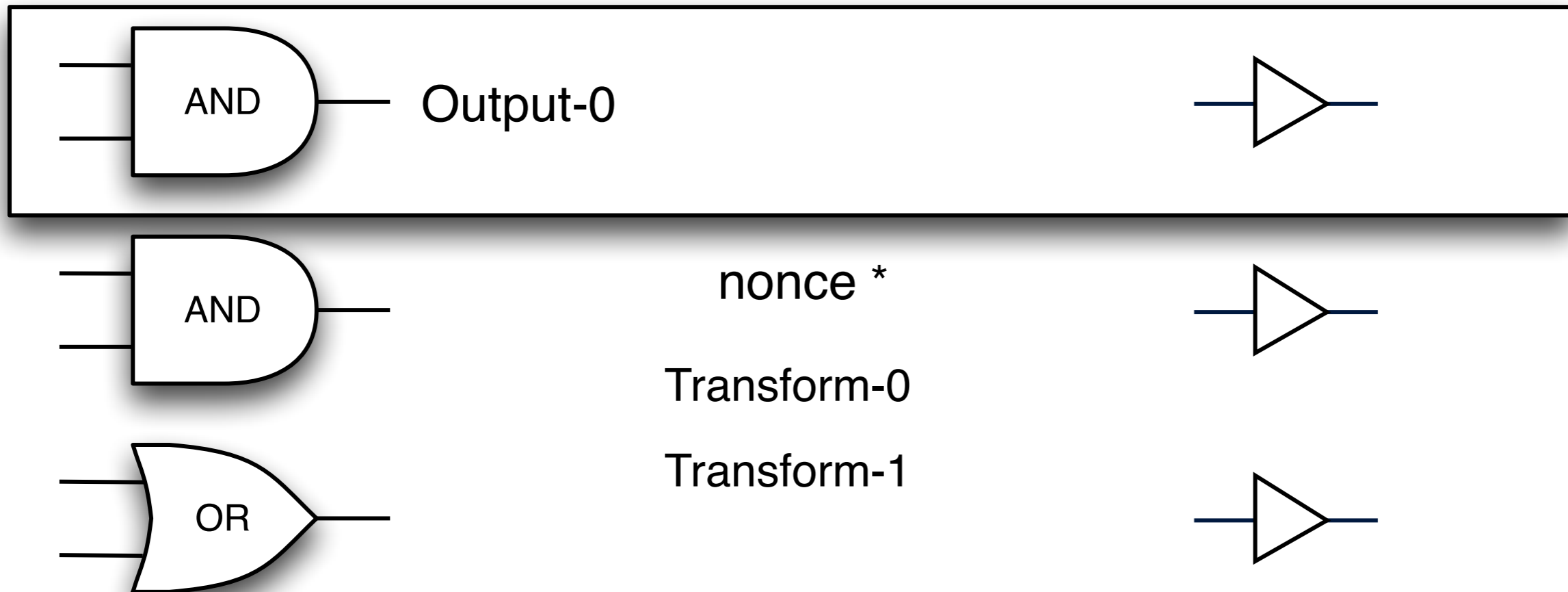


Transform-1



\* = once per circuit

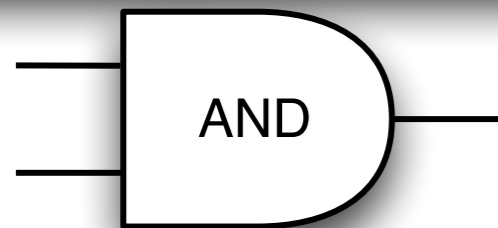
## Evaluator



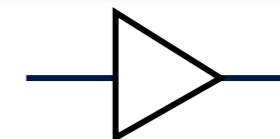
$$\text{Random-0} = \text{hash}(\text{Output-0} \oplus \text{nonce}) \oplus \text{Transform-0}$$

\* = once per circuit

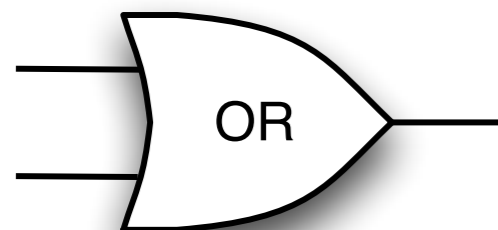
## Evaluator



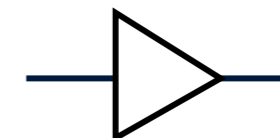
nonce \*



Transform-0



Transform-1



$$\text{Random-0} = \text{hash}(\text{Output-0} \oplus \text{nonce}) \oplus \text{Transform-0}$$

\* = once per circuit

# How to check?



- Evaluator can save the possible out values for a check circuit and upon receiving the next iteration of that check circuit can verify the transformation is correct.

- **Problem:**

In our base protocol both parties know the check and evaluation split allowing the generator to only disrupt evaluation gates unless we commit.

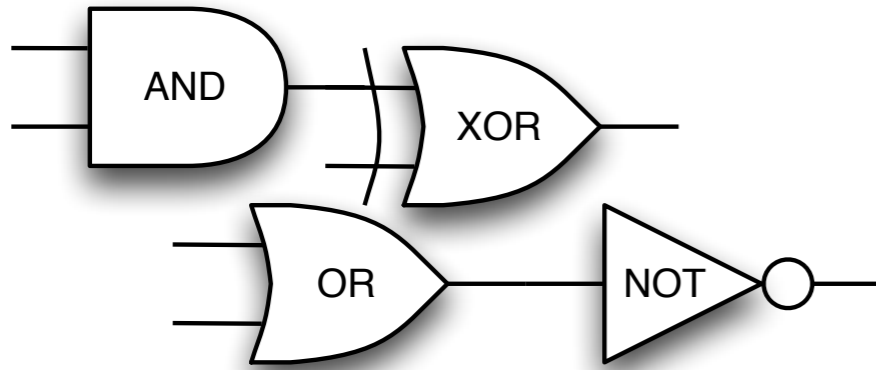
- If we commit ahead of time we introduce other problems of longevity of the values.



- If the generator does not know the evaluation circuits from the check circuits, then he has to send correct transformation gates for all circuits.
- This also means the generator, for the entirety of the computation, can never learn the split.

# Multiple Cut and Choose

Garbled Circuit 1



Check Circuit

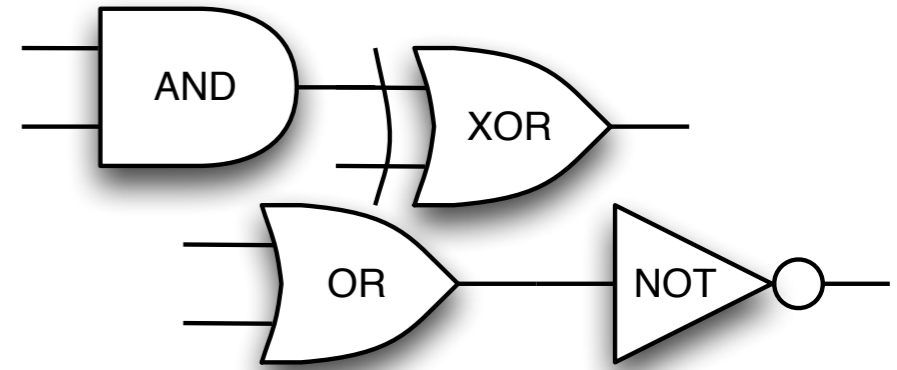
Evaluation Circuit

Check Circuit

Evaluation Circuit

Check Circuit

Garbled Circuit 2



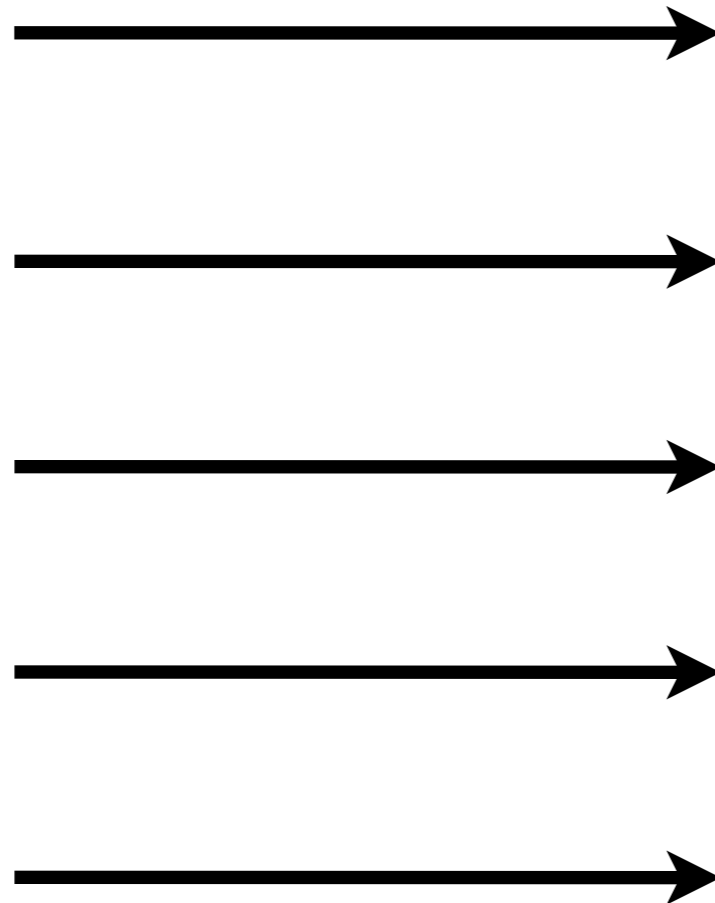
Evaluation Circuit

Check Circuit

Check Circuit

Check Circuit

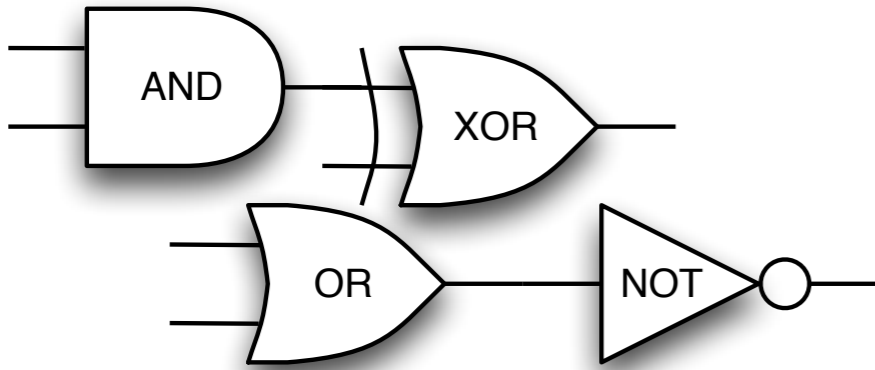
Evaluation Circuit



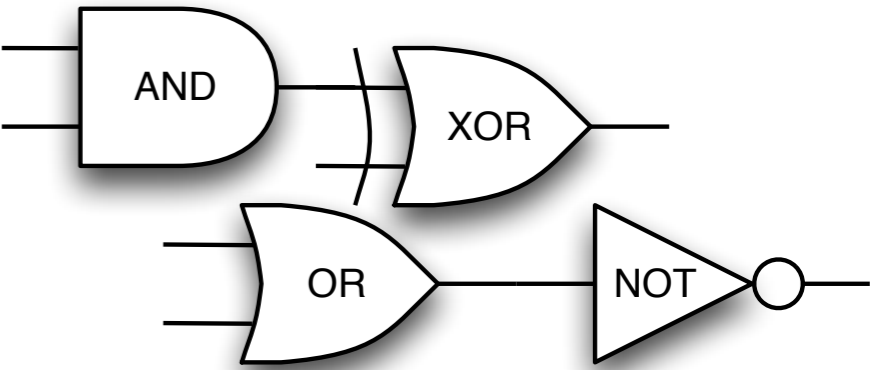


# Multiple Cut and Choose

Garbled Circuit 1



Garbled Circuit 2



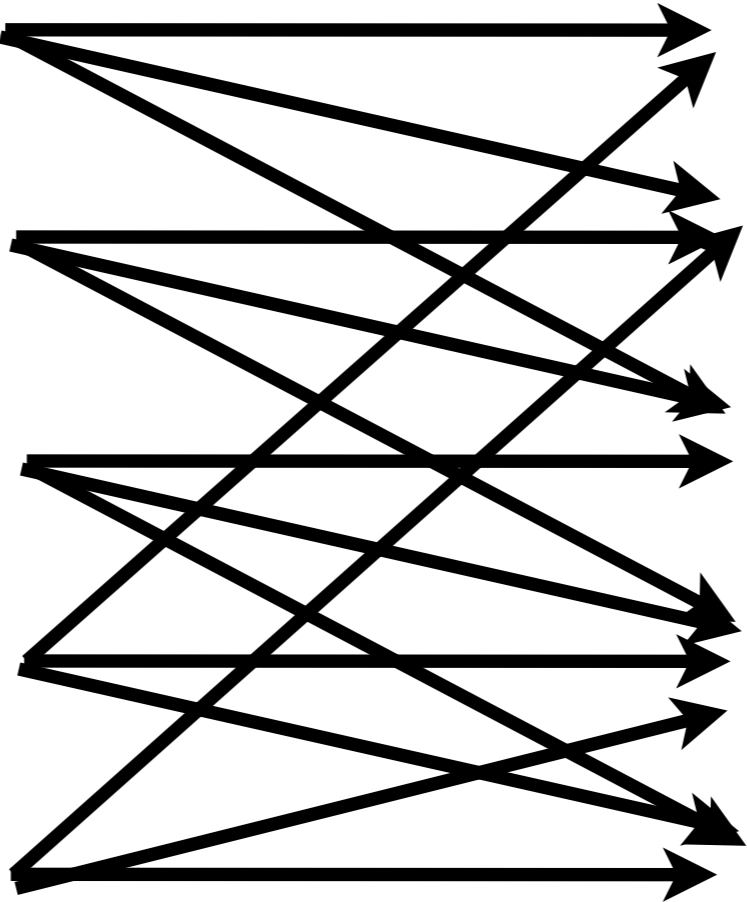
Check Circuit

Evaluation Circuit

Check Circuit

Evaluation Circuit

Check Circuit



Evaluation Circuit

Check Circuit

Check Circuit

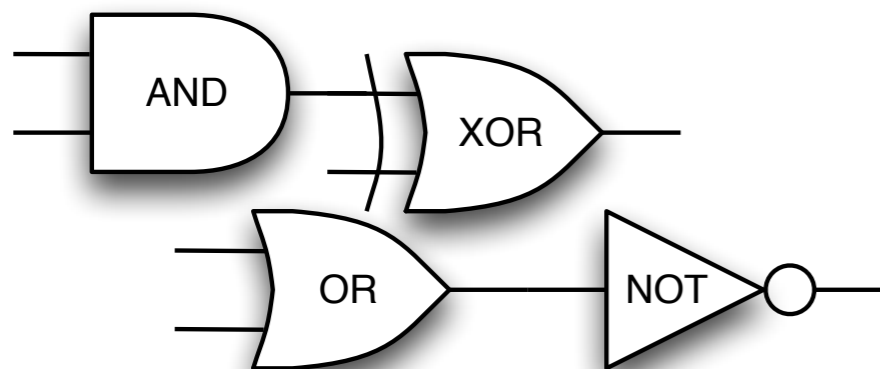
Check Circuit

Evaluation Circuit

# Single Cut and Choose



Garbled Circuit 1



Check Circuit

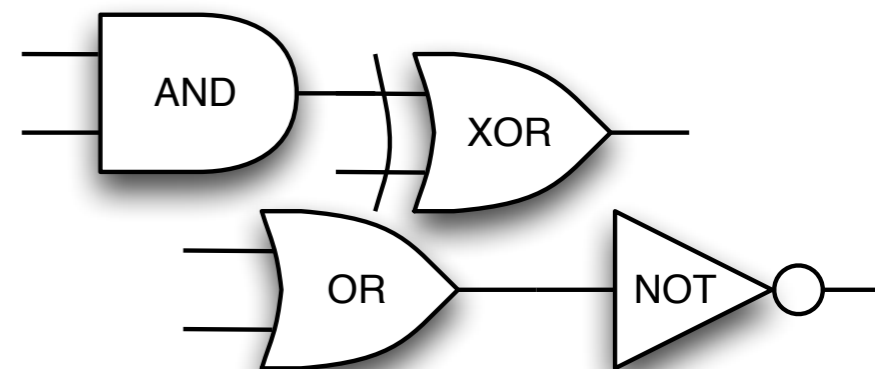
Evaluation Circuit

Check Circuit

Evaluation Circuit

Check Circuit

Garbled Circuit 2



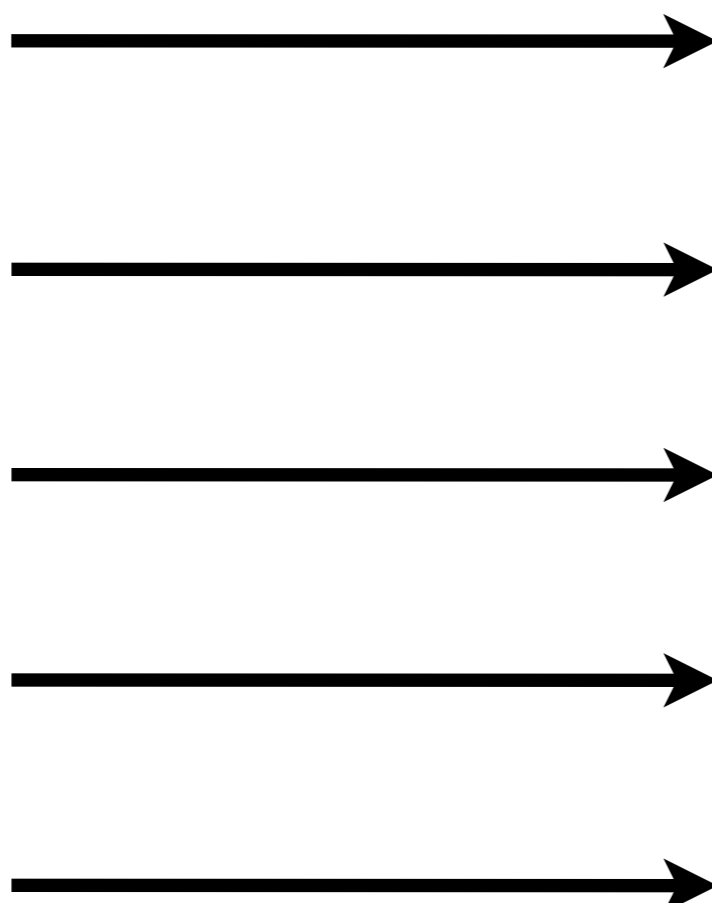
Check Circuit

Evaluation Circuit

Check Circuit

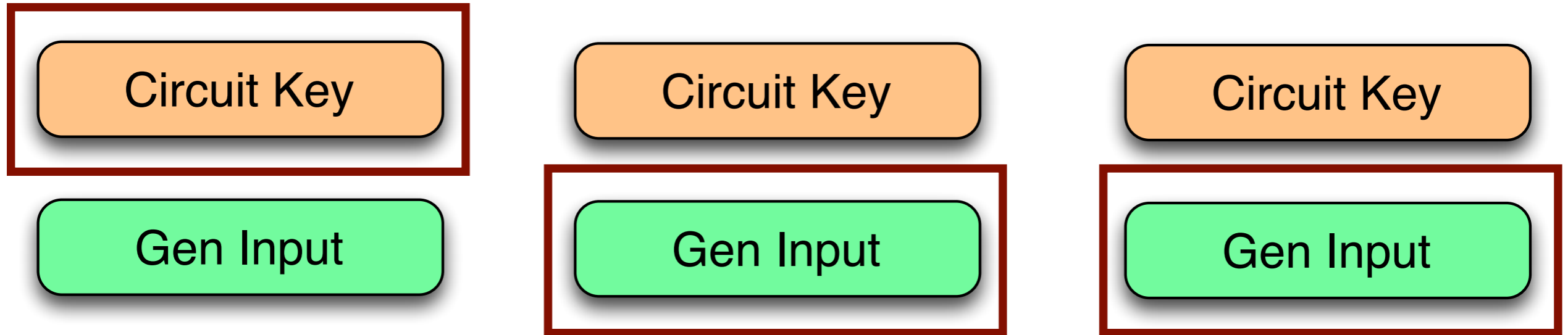
Evaluation Circuit

Check Circuit



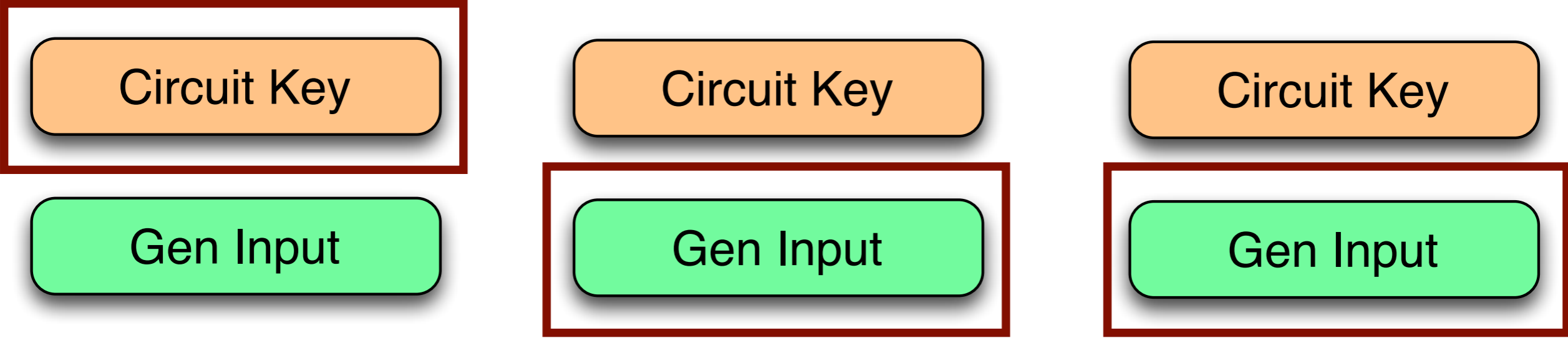
- For the cut and choose, we use OT to select encryption keys as implemented in [SS13].
- In the first computation perform the cut and choose.
- In any subsequent computation use the encryption keys to generate new encryption keys.

# 3 Circuit Example

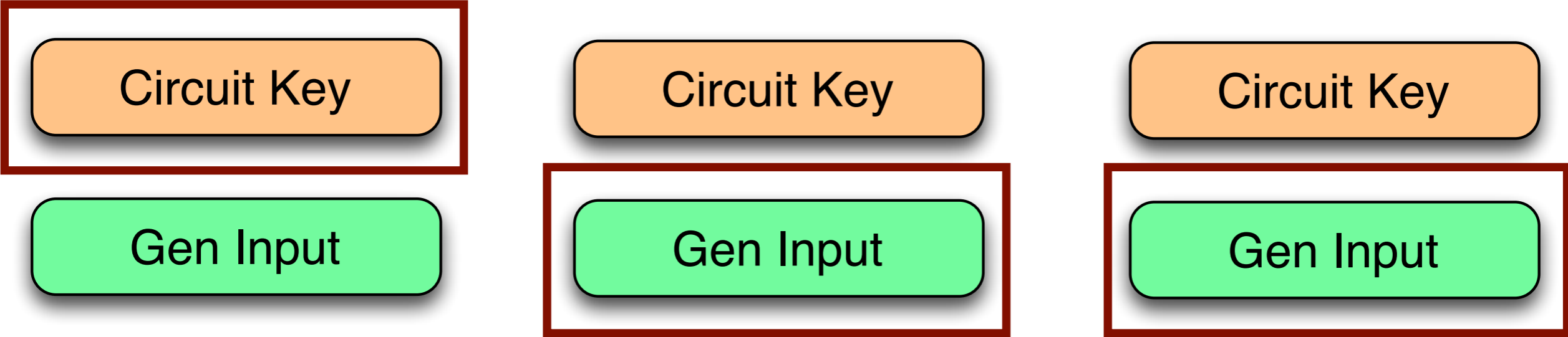


Cut and Choose via OT

# 3 Circuit Example



## Cut and Choose via OT



# Checking Transformations

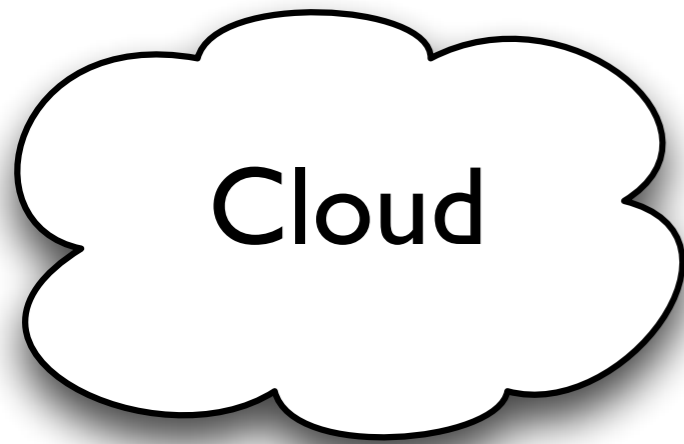


- Generator never learns the check/evaluation circuits
- Evaluator can check how the generator transforms values from one garbled circuit computation to another garbled circuit computation.

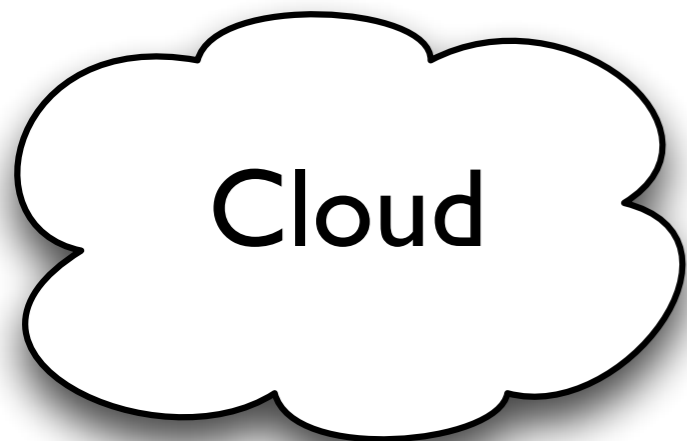


- Server-aided setting
- [CMTB13] system: Outsources the evaluation of a garbled circuit from a mobile device to a high performance server (cloud) with security guarantees.
- Based on [KSS12]

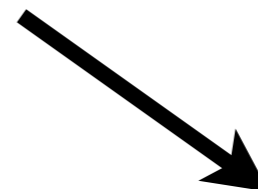
## Generator



## Evaluator

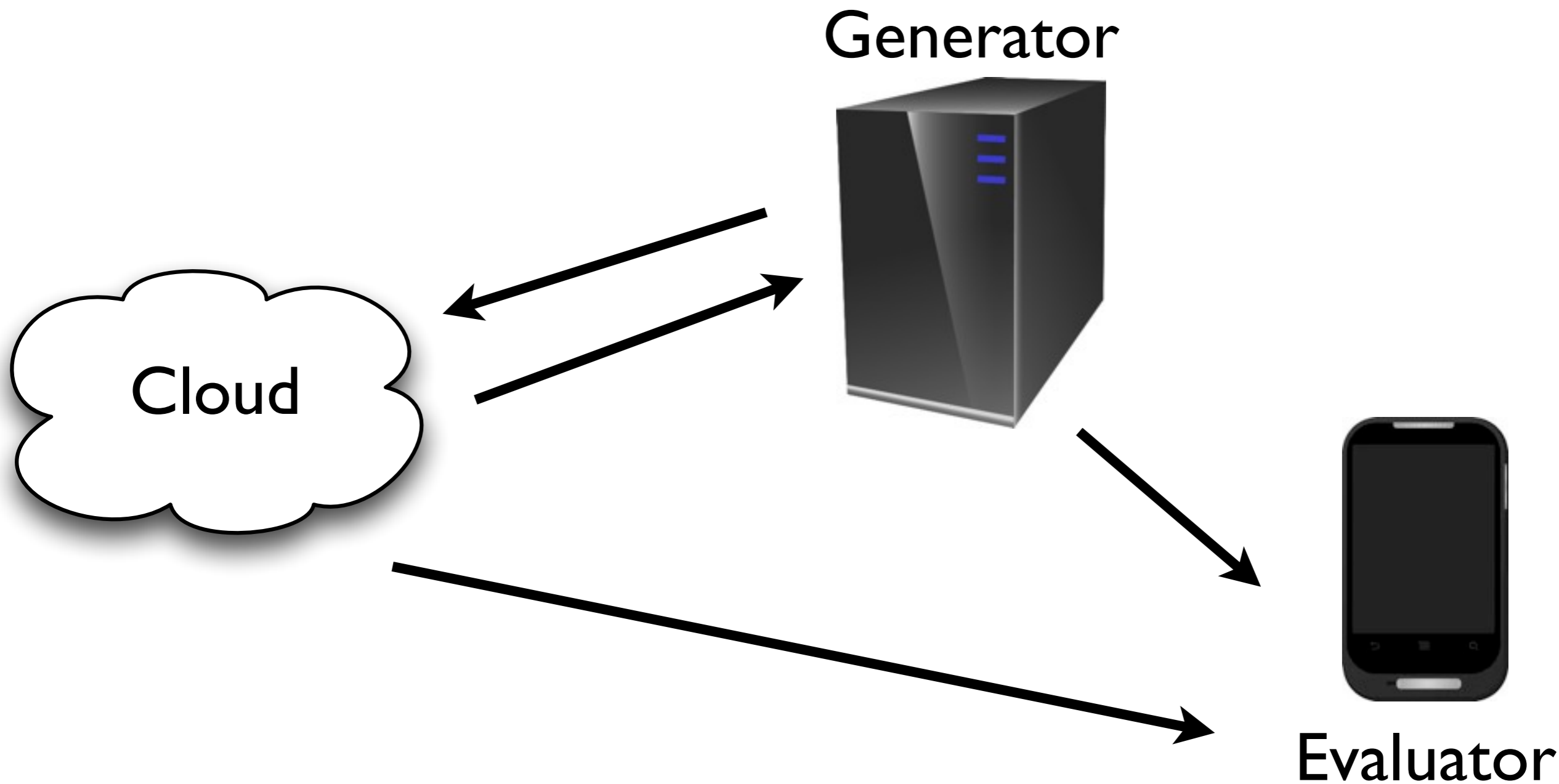


## Generator

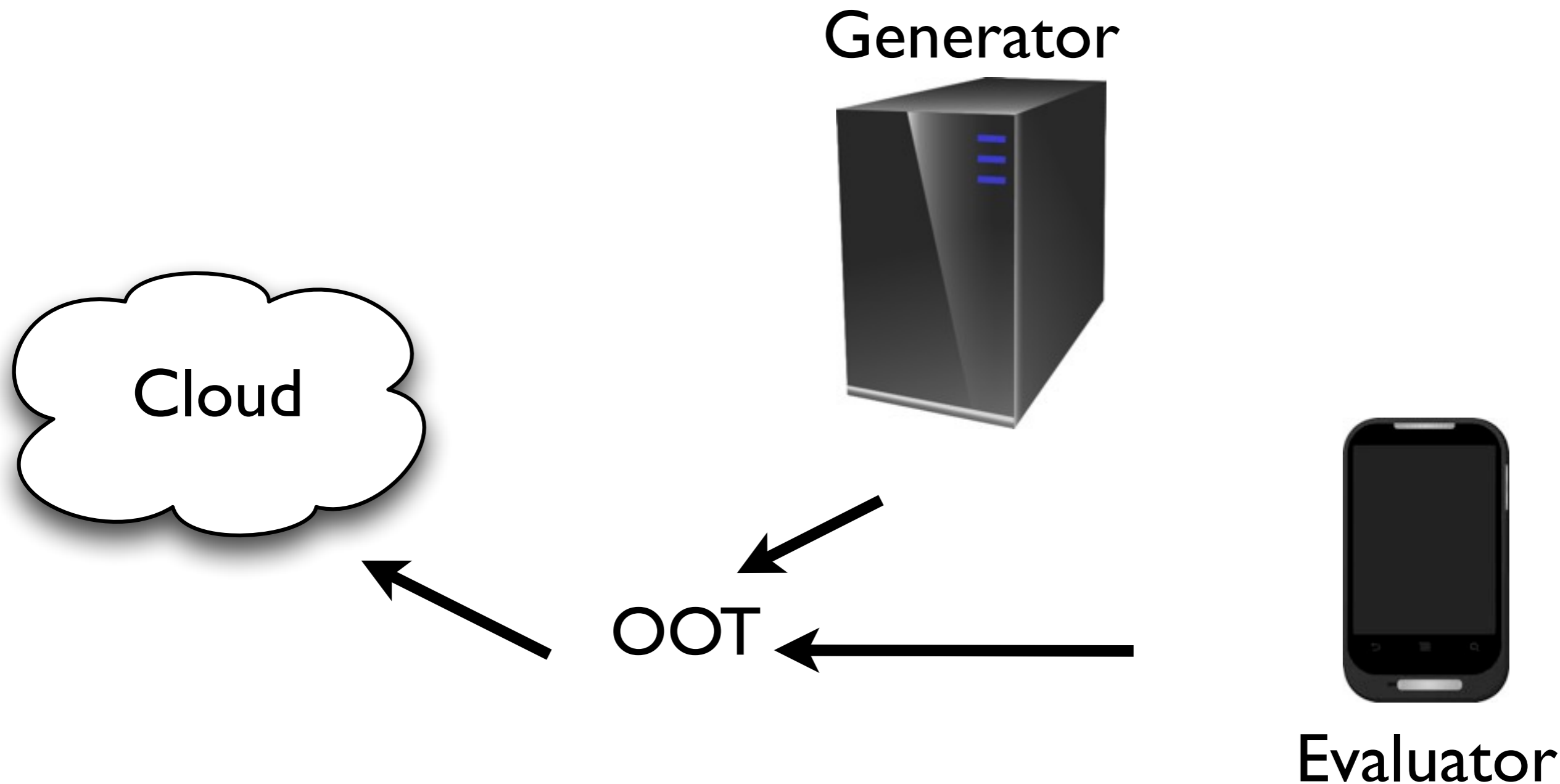


## Evaluator

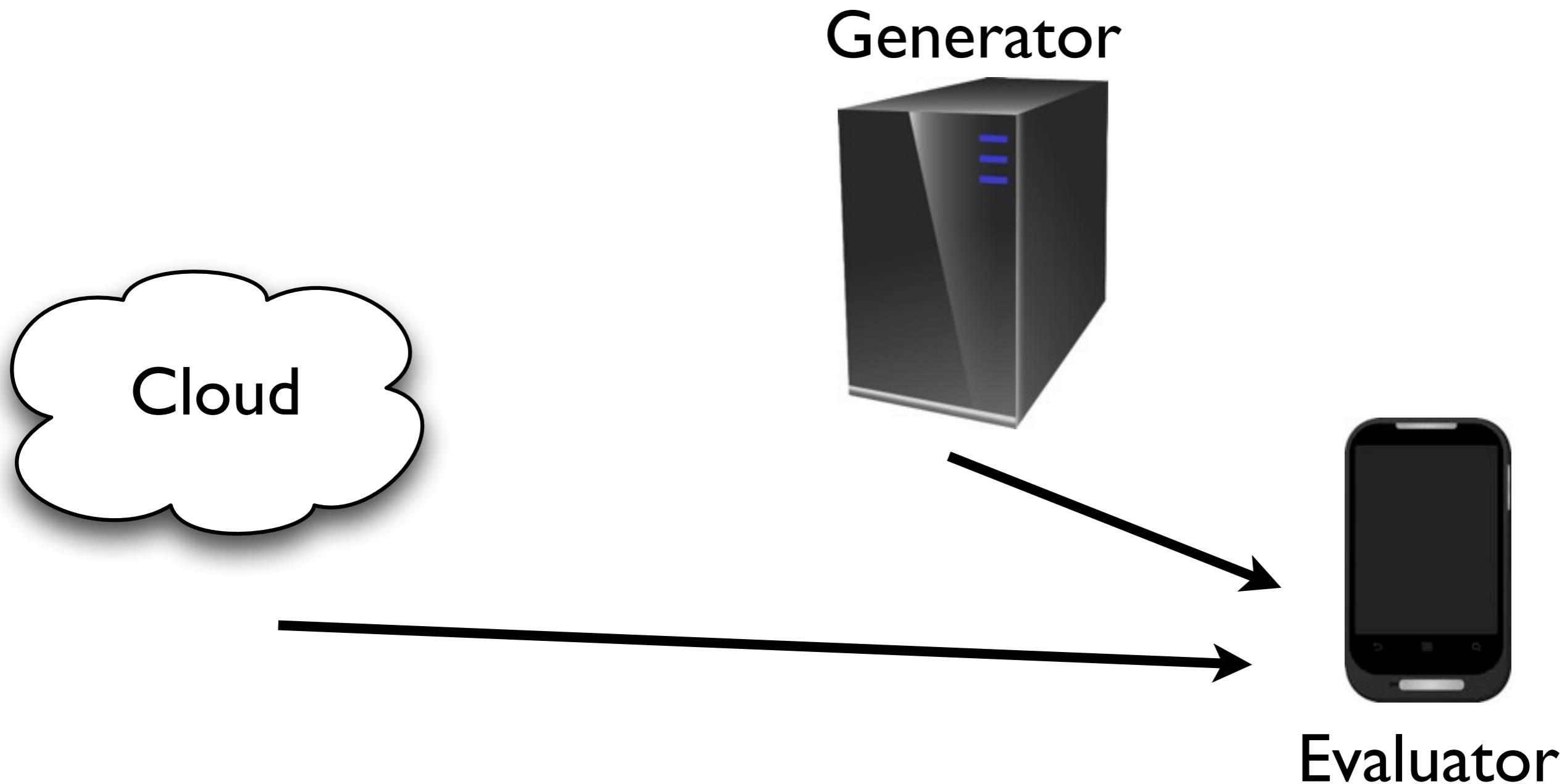
# Circuit Commit



Cut and Choose

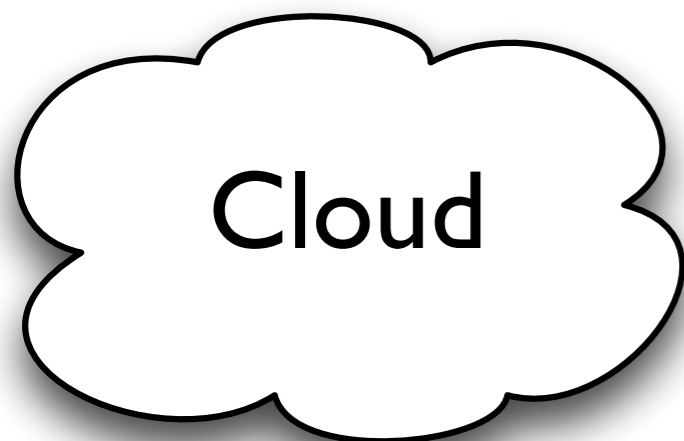
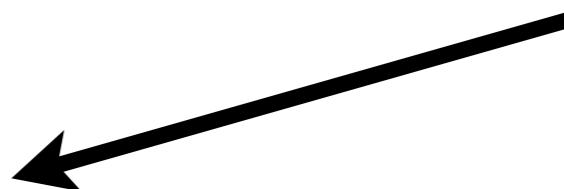


## Outsourced Oblivious transfer



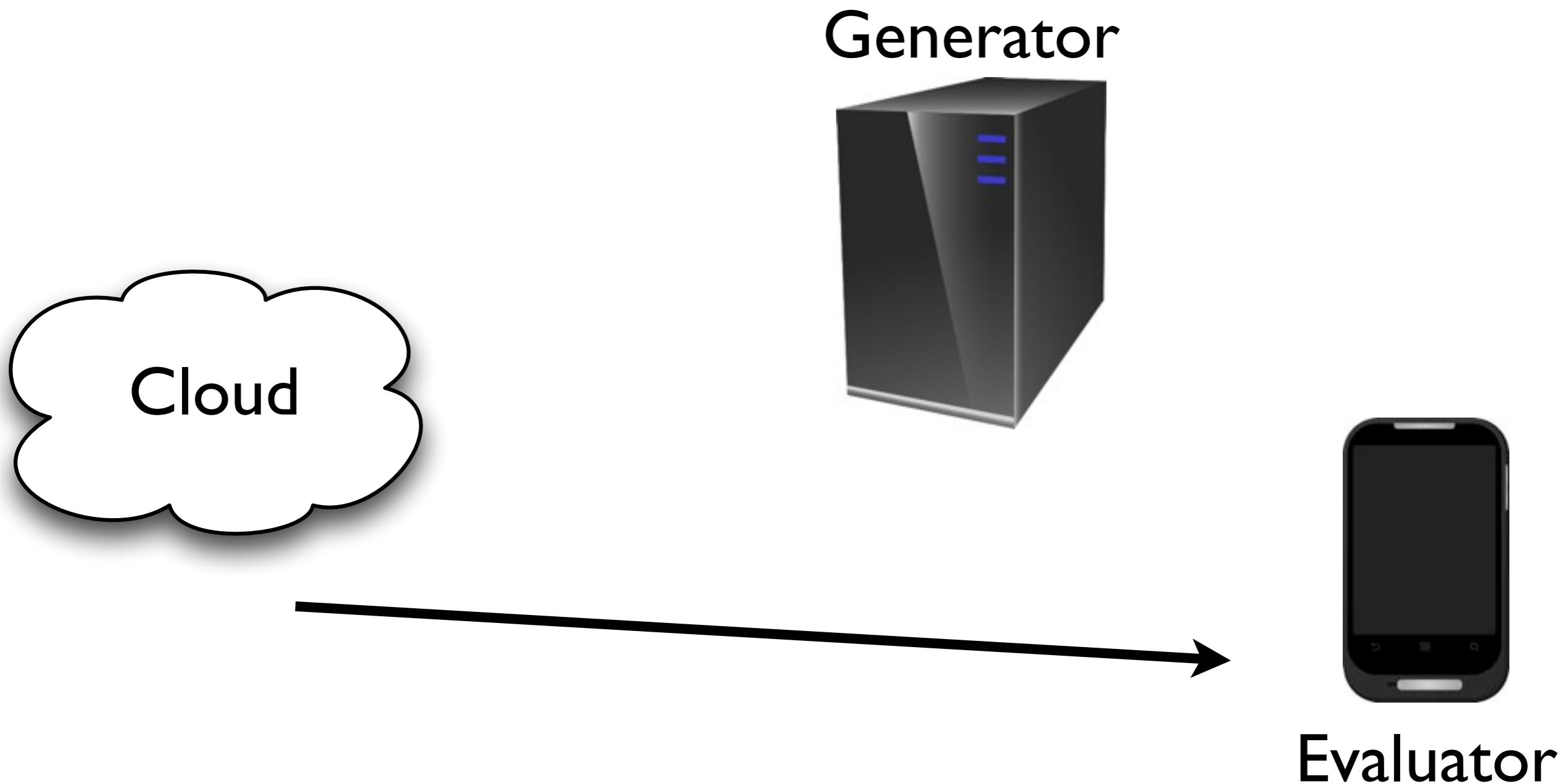
**Generator's Input  
Consistency Check**

## Generator



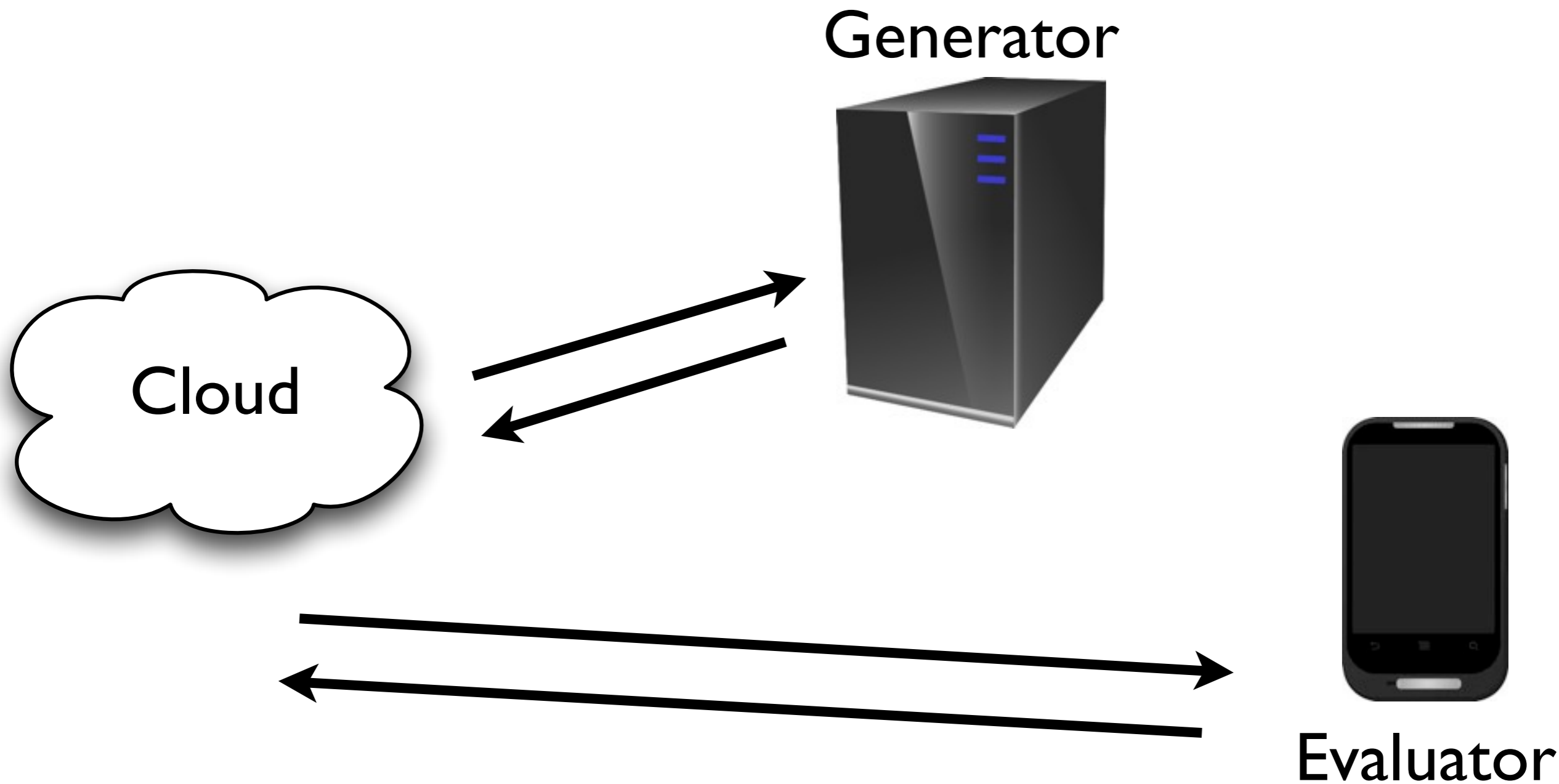
## Evaluator

# Circuit Evaluation



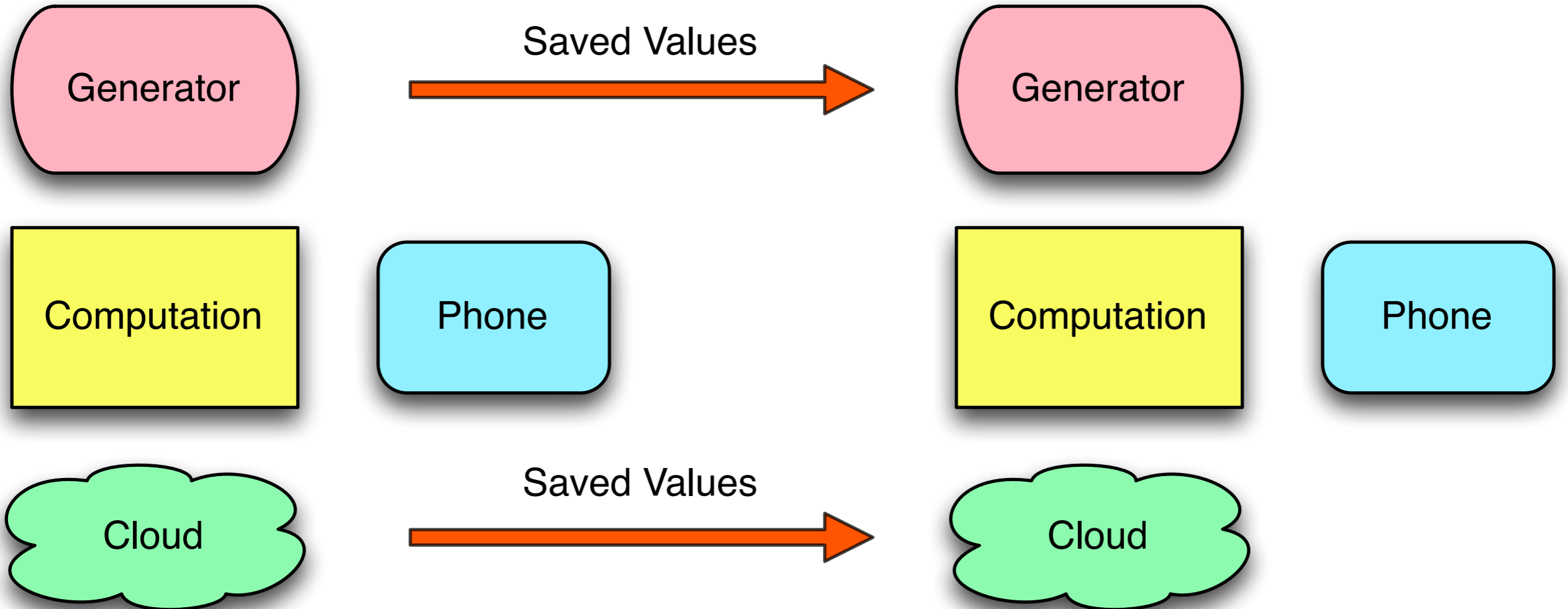
## Circuit Commitment Check





Output and Output check

# Outsourced PartialGC



# Protocol



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Generator

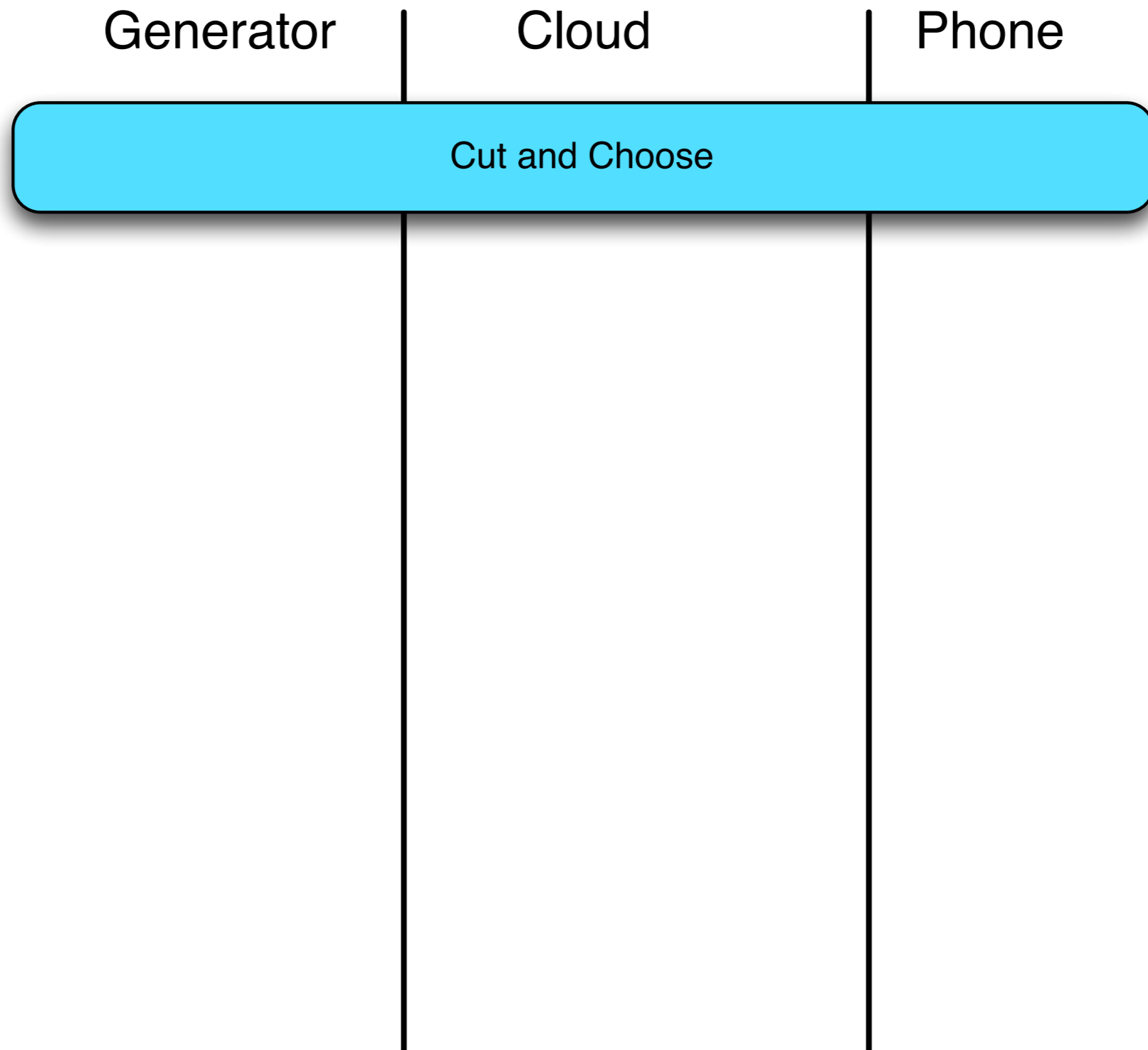
Cloud

Phone

# Protocol



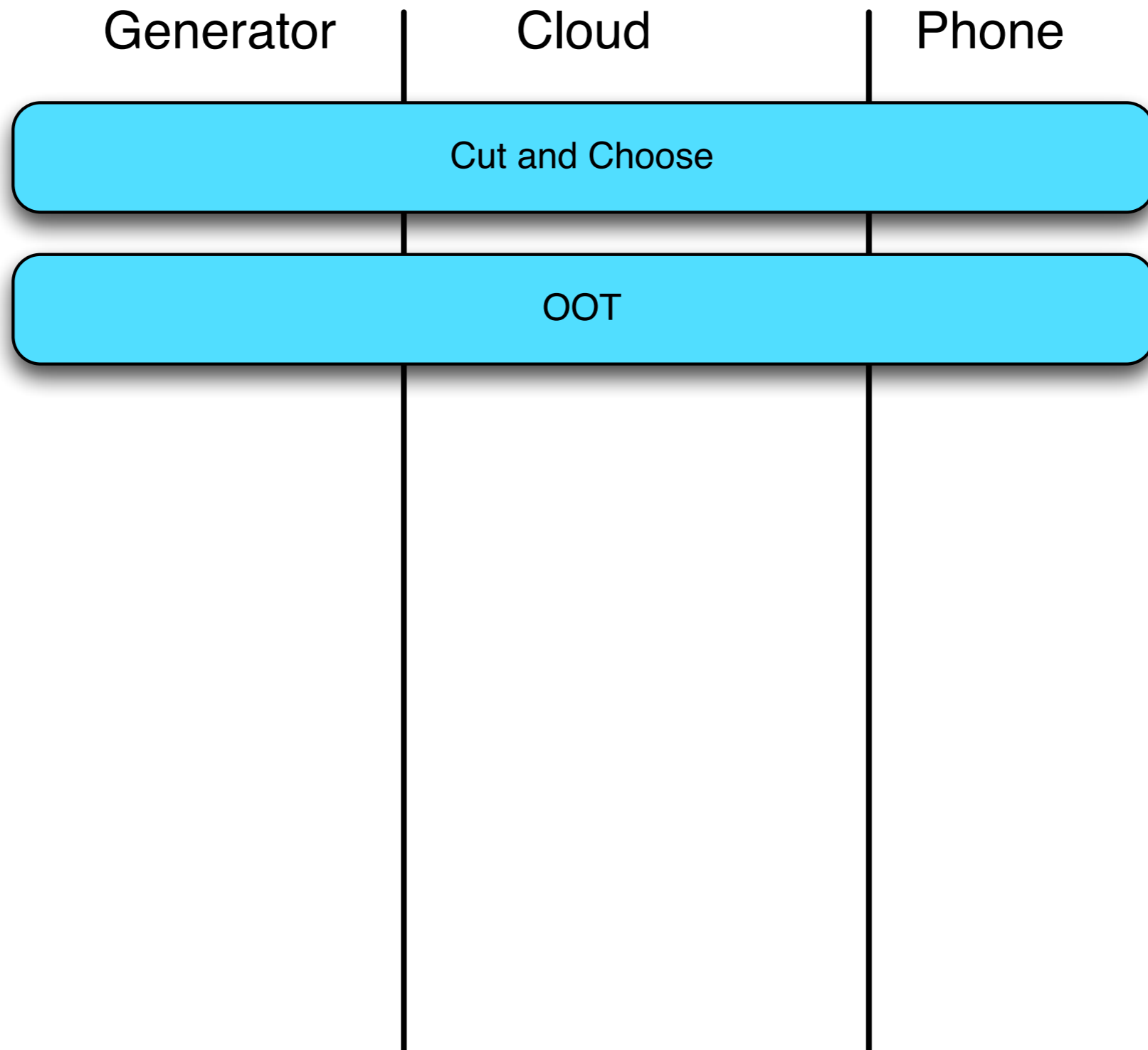
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# Protocol



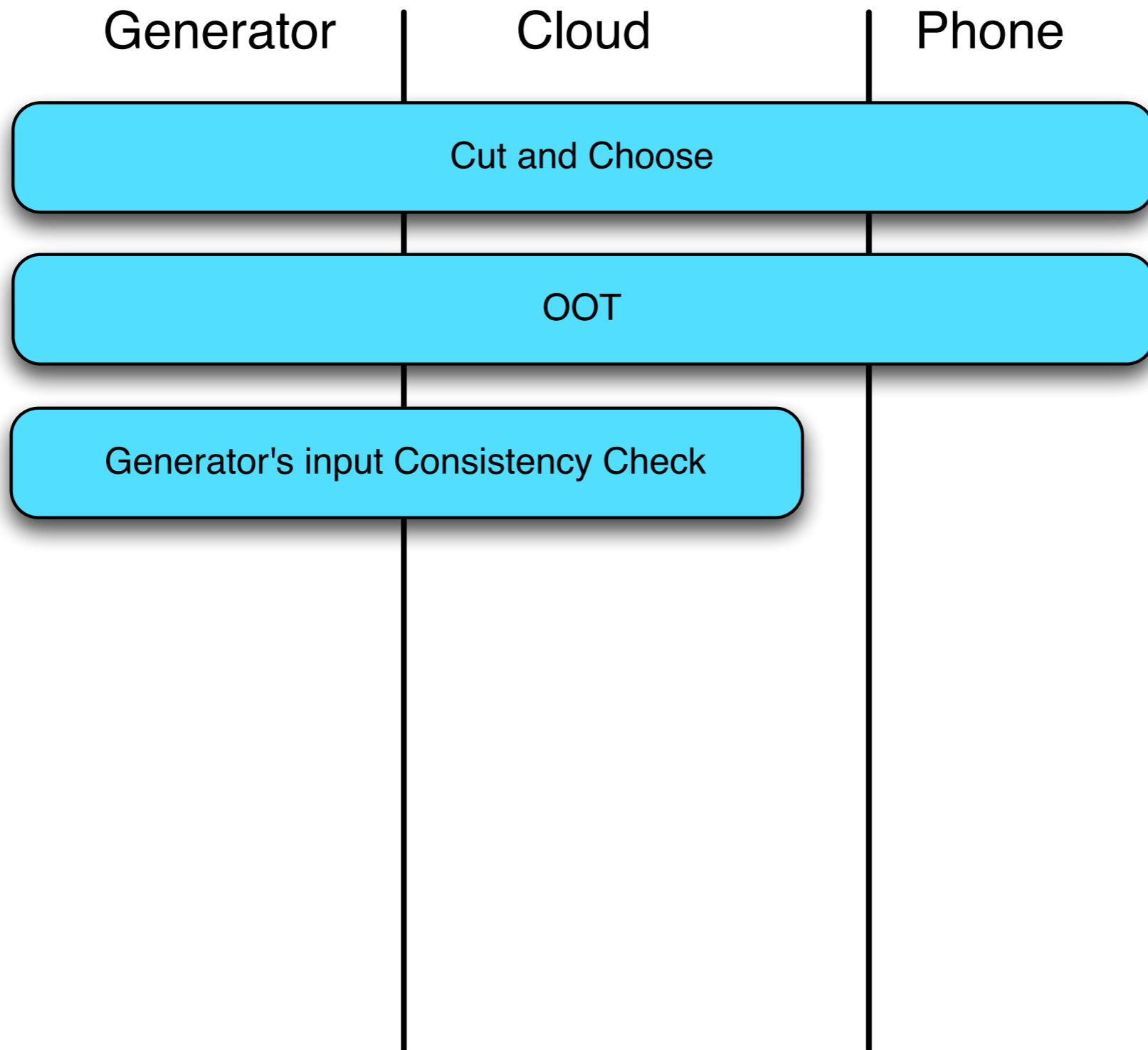
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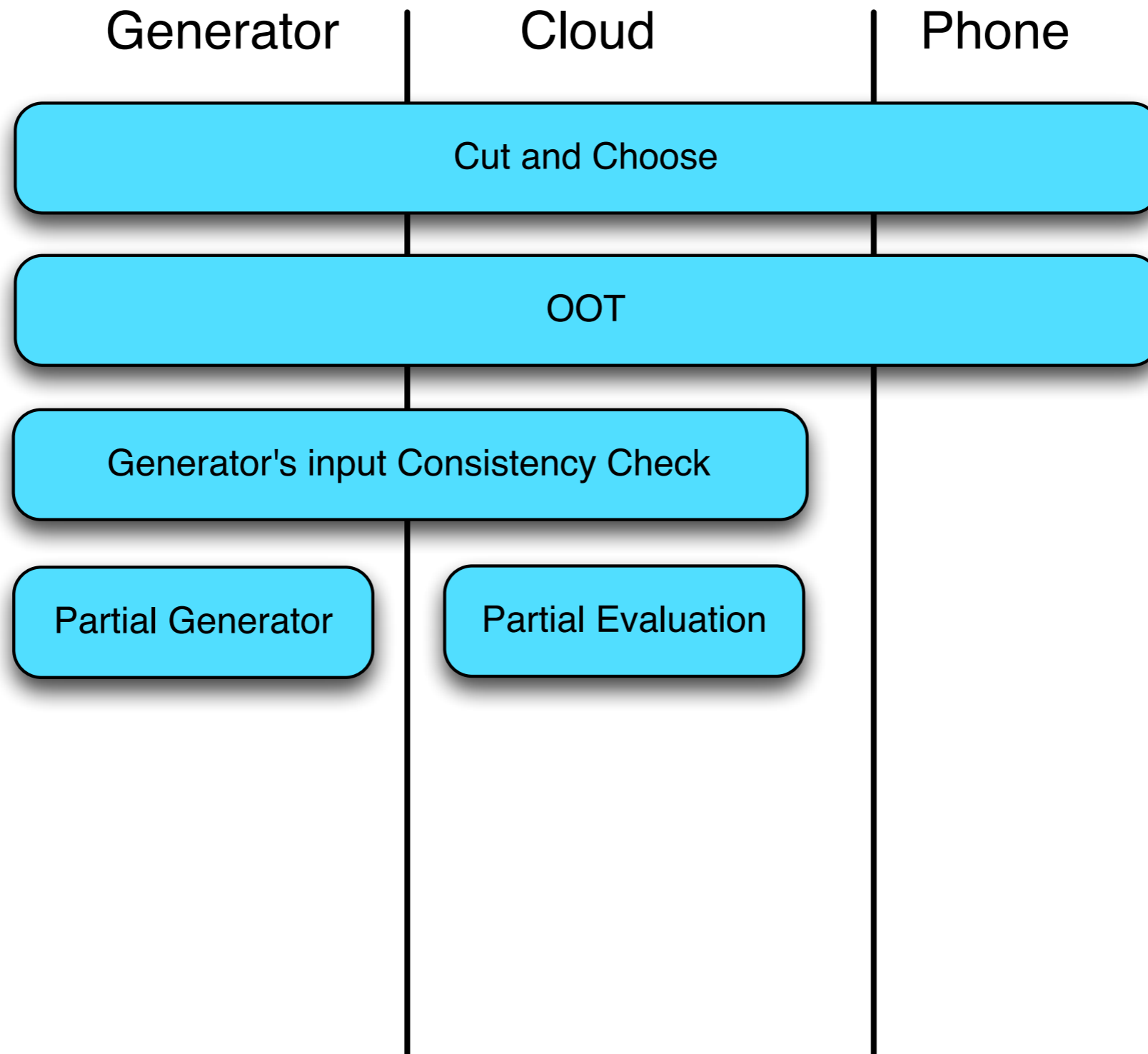
# Protocol



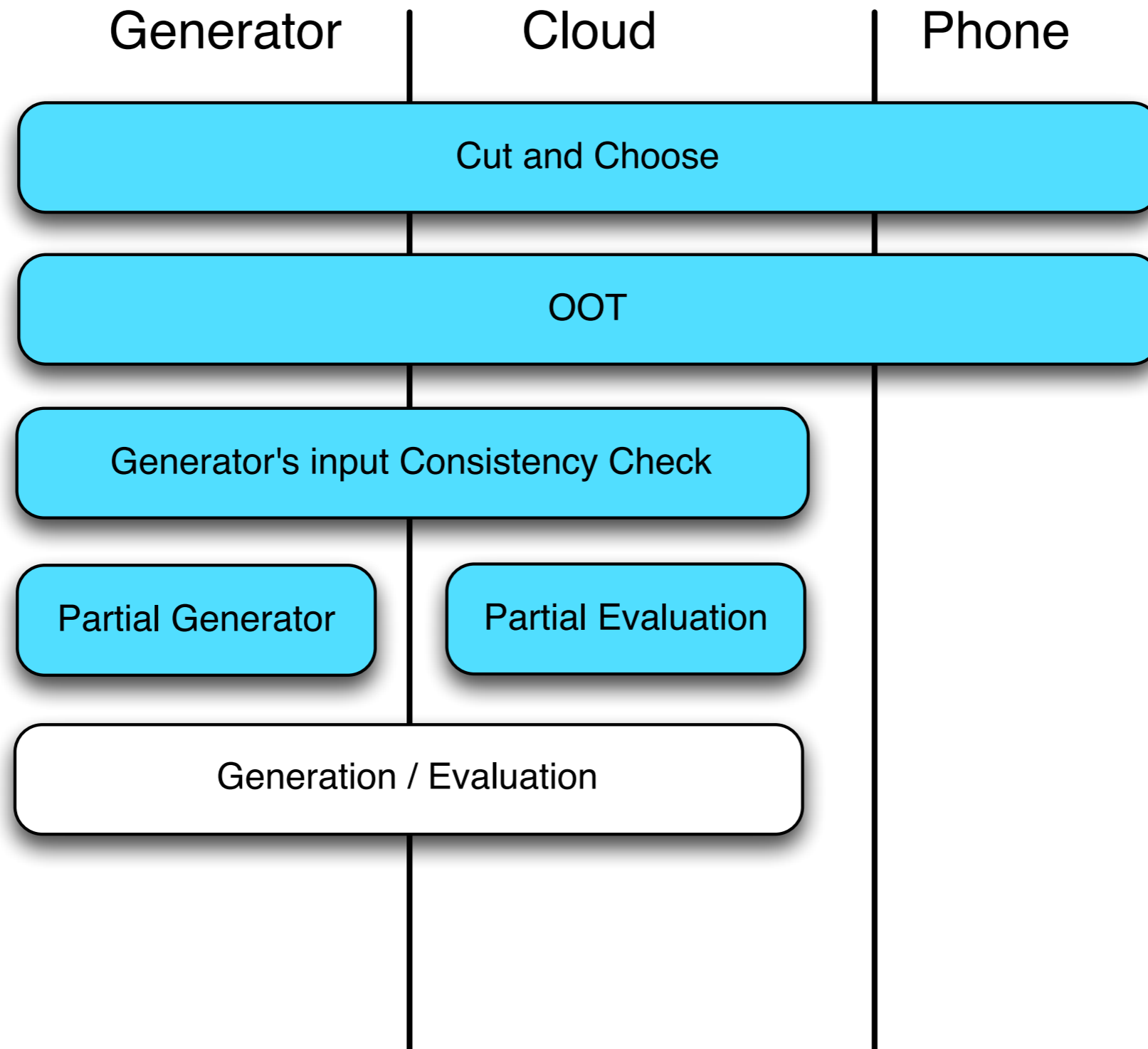
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# Protocol

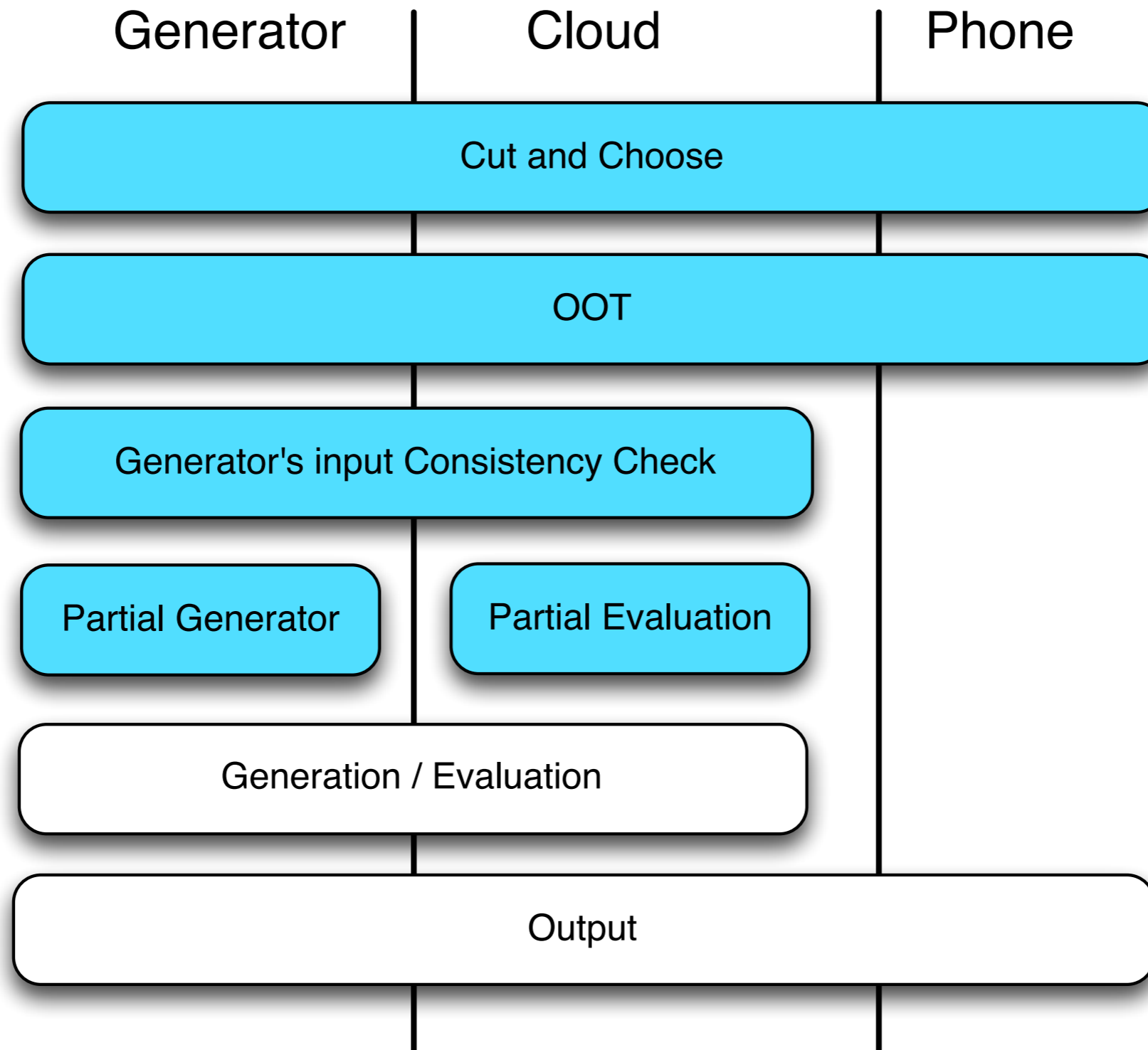


# Protocol

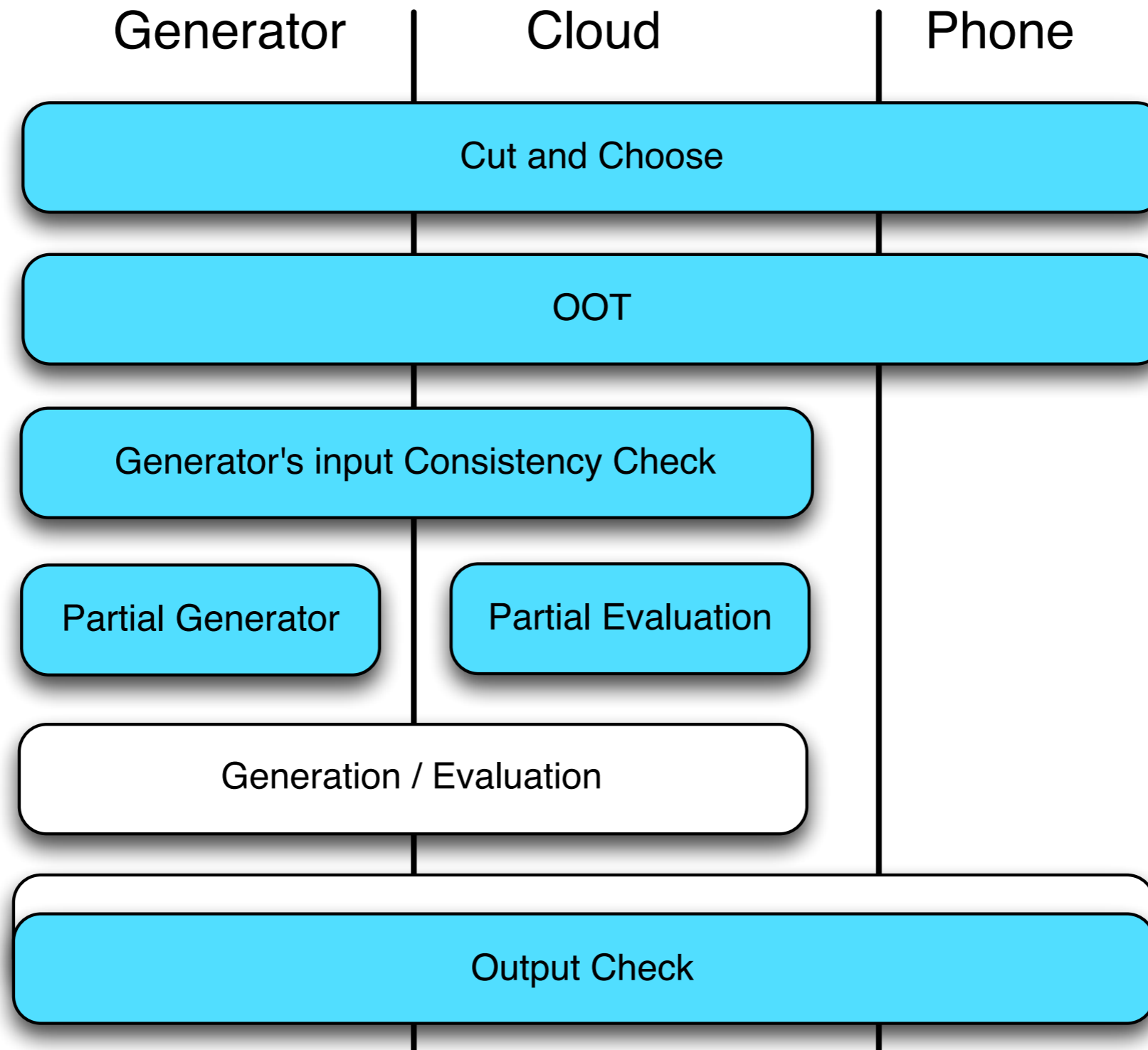




# Protocol



# Protocol



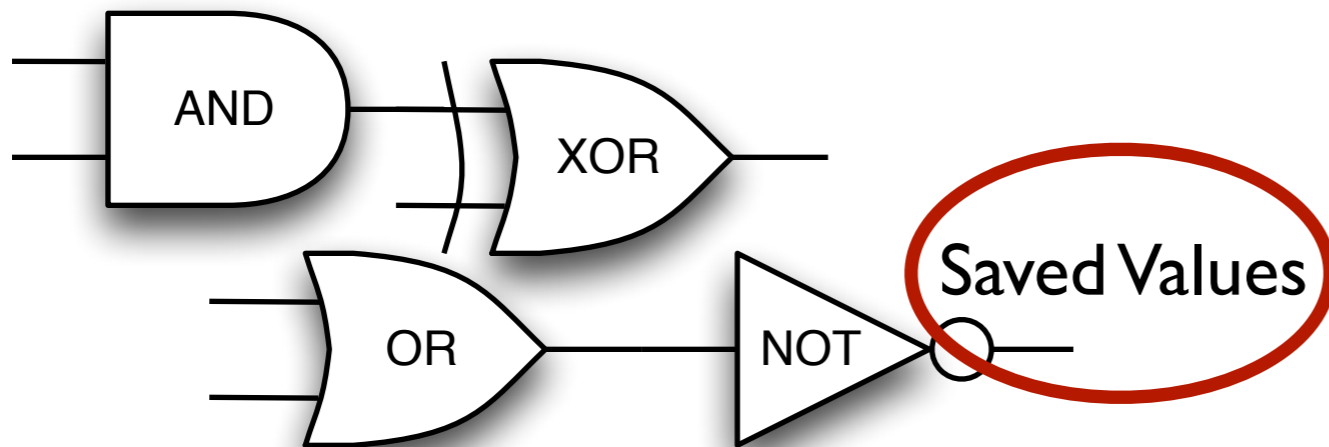
- Output (  $x \parallel \text{MAC}(x)$  )
- Slower for circuit evaluation. Proof of concept implementation has  $\sim 14,000$  non-XOR gates per 128 bits.
- Extremely fast for our outsourcing party [ bits/128 MAC operations instead of the output proof with homomorphic XOR commitments].

# Wrong Saved Values

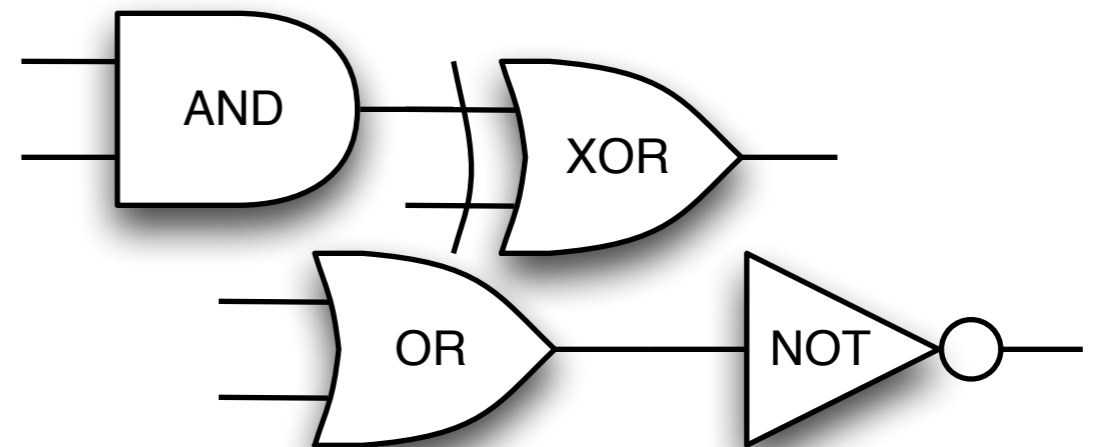


- Generator gets caught through circuit check
- Cloud gets caught, assuming he continues in the computation, when the output check fails

Garbled Circuit 1



Garbled Circuit 2



# Incorrect Check Circuits



- Aborting on incorrect check circuits gives away information about what circuits are checked or evaluated.
- If a check is found to be incorrect, then the remaining computation and any saved values must be abandoned.
- Cloud informs the Generator and Phone of the incorrect circuit and what it should have been.



# Preliminary Test Results



	64 Circuits			256 Circuits		
	CMTB	Partial		CMTB	Partial	
KeyedDB 64	$72 \pm 2\%$	$8.3 \pm 5\%$	8.7x	$290 \pm 2\%$	$26 \pm 2\%$	11x
KeyedDB 128	$140 \pm 2\%$	$9.5 \pm 4\%$	15x	$580 \pm 2\%$	$31 \pm 3\%$	19x
KeyedDB 256	$270 \pm 1\%$	$12 \pm 6\%$	23x	$1200 \pm 3\%$	$38 \pm 5\%$	32x

\* both evaluated on same hardware, security parameters, and setup

# Work in progress



	64 Circuits			256 Circuits		
	CMTB	Partial		CMTB	Partial	
Largest Substring 128	190 ± 4%	20 ± 9%	9.5x	800 ± 7%	84 ± 9%	9.5x
Largest Substring 256	370 ± 4%	40 ± 10%	9.3x	1700 ± 8%	130 ± 7%	13x
Largest Substring 512	730 ± 4%	70 ± 10%	10x	-	200 ± 10%	-

- For comparison
  - In [CMTB] output and input values under a 1-time pad with MACs.

- Saving wire labels
- Transform and check values
- Discussed our protocol and preliminary results
- Work in progress ...



# Questions?



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# Questions?



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